



lawphysics
Latin American Webinars on Physics

Connecting neutrinos with light dark matter candidates

Roberto A. Lineros

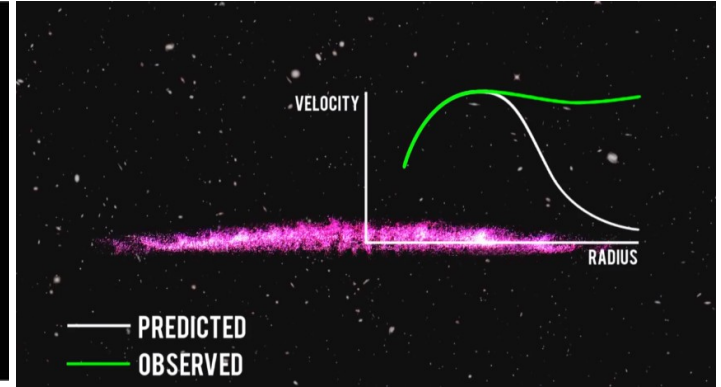
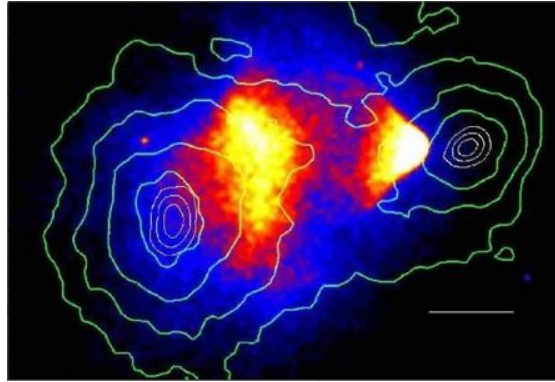
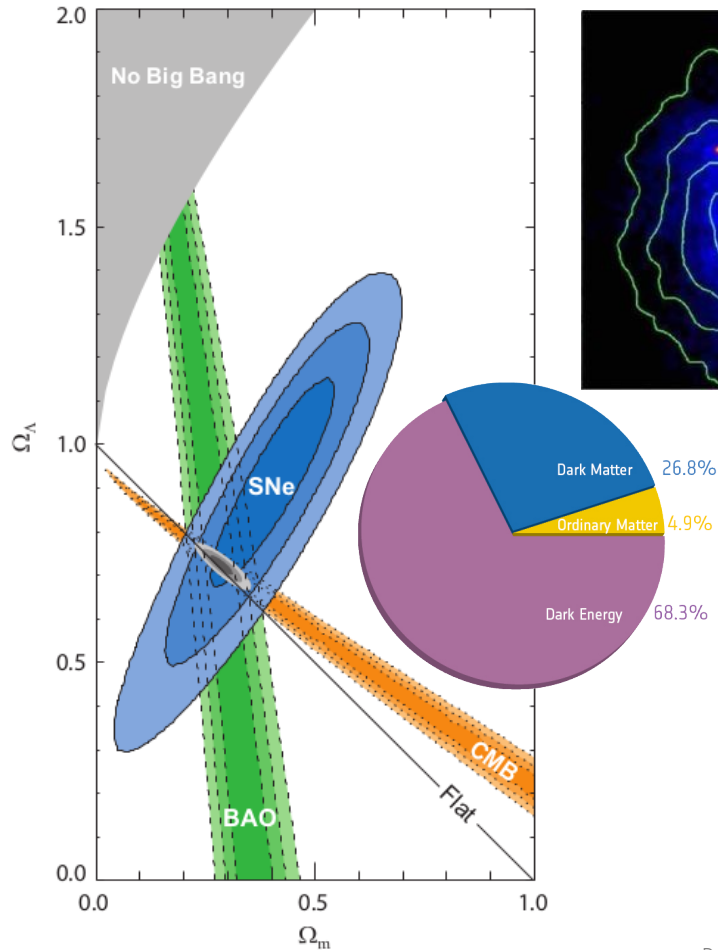
Space sciences, Technologies and Astrophysics Research (STAR) Institute
Université de Liège

Dark Matter Days 2017 – CIFFU BUAP

Outline



Dark Matter

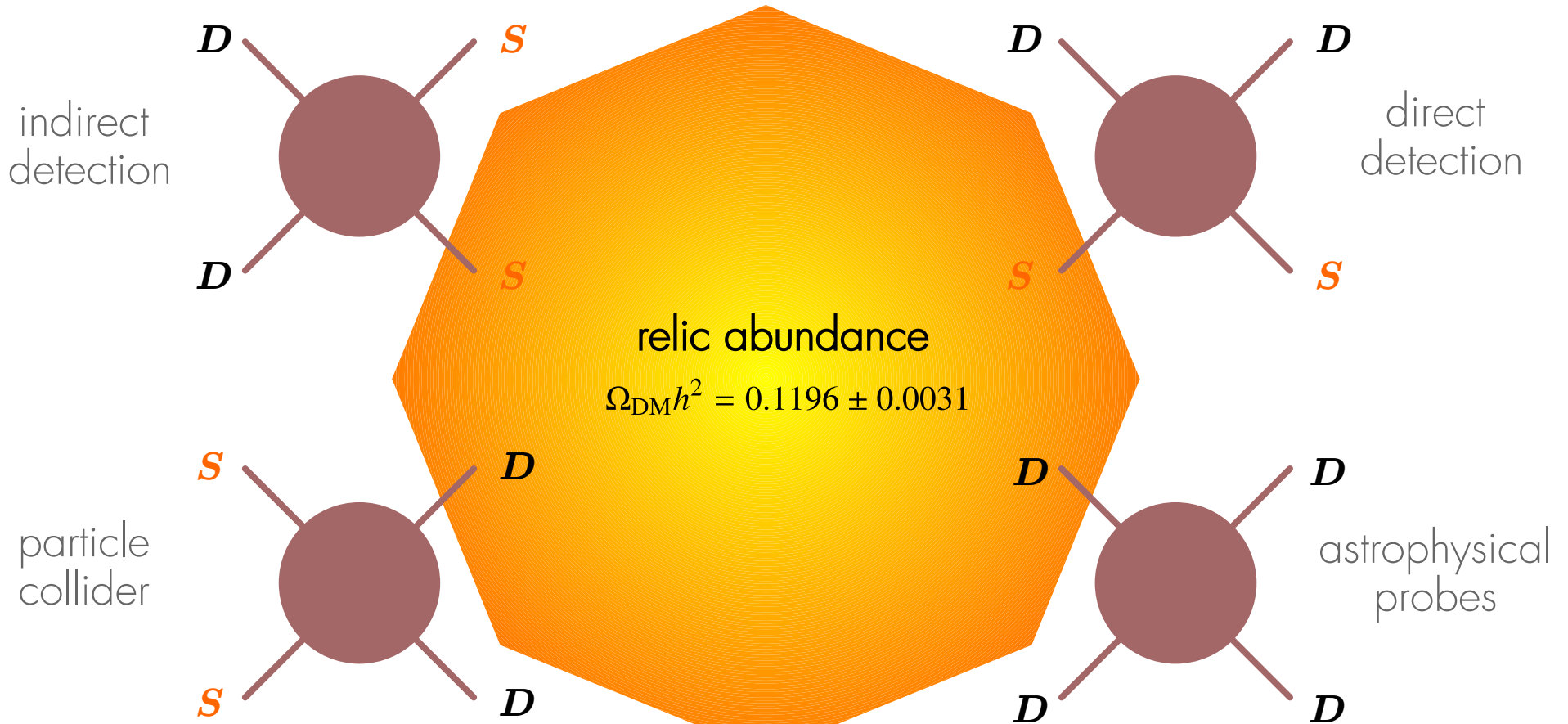


Observations support Dark Matter

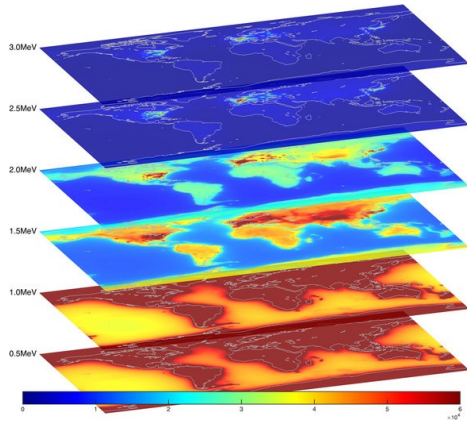
- Dynamics of clusters and galaxies
- Structure formation
- CMB anisotropies
- Baryon Acoustic Oscillation

$$\Omega_{\text{DM}} h^2 = 0.1196 \pm 0.0031$$

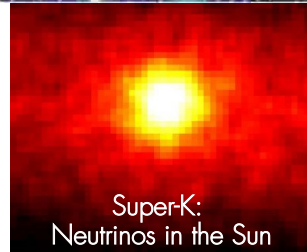
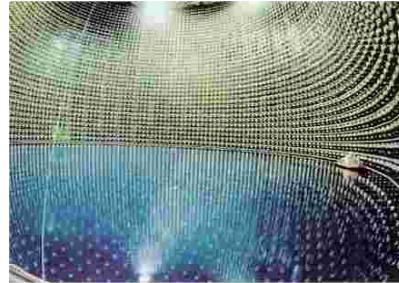
Dark Matter Searches



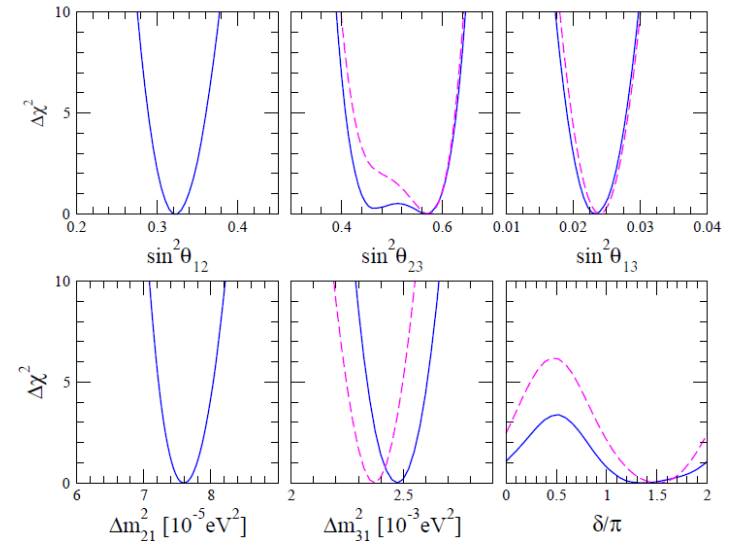
Neutrinos



AGM2015: Antineutrino Global Map 2015



Forero, Tortola and Valle PRD 90 (2014) 093006



The **SM** predicts zero neutrino mass

Beyond SM physics is required to explain mass spectrum and mixing angles

Example 1

(light) Dark Matter candidate
and neutrino masses

Neutrino mass mechanisms

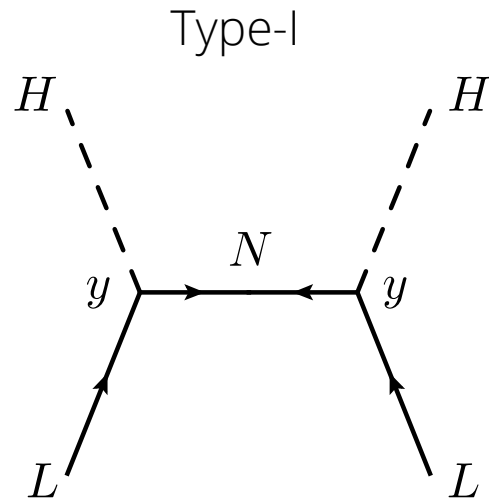
A large fraction of the models uses the 5-dim **Weinberg operator** to generate **majorana** neutrino masses

$$\mathcal{O}_{5ij} \propto (L_i H)^T (L_j H)$$

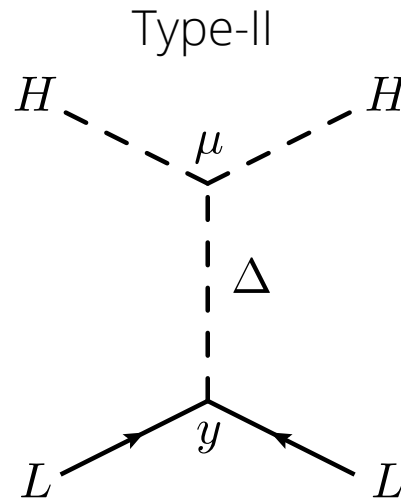
This operator breaks lepton number in **2 units**

Neutrino mass mechanisms

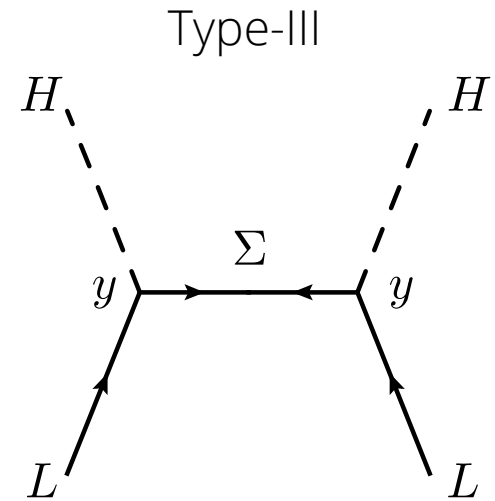
The commonly known schemes are **see-saw mechanisms**



$$m_\nu \propto \frac{v^2 y^2}{M_N}$$



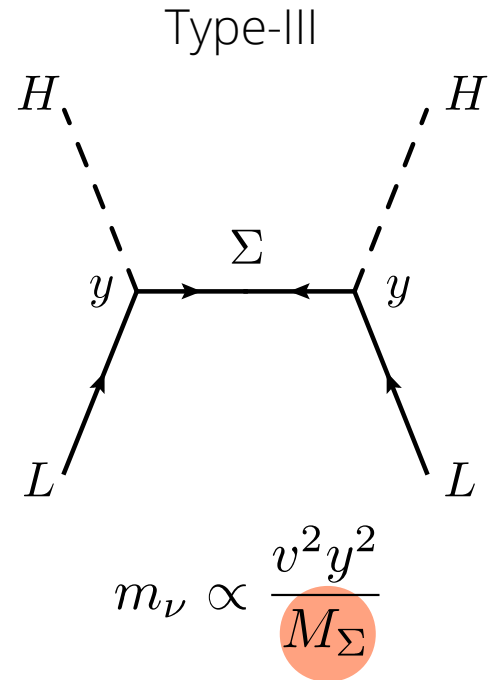
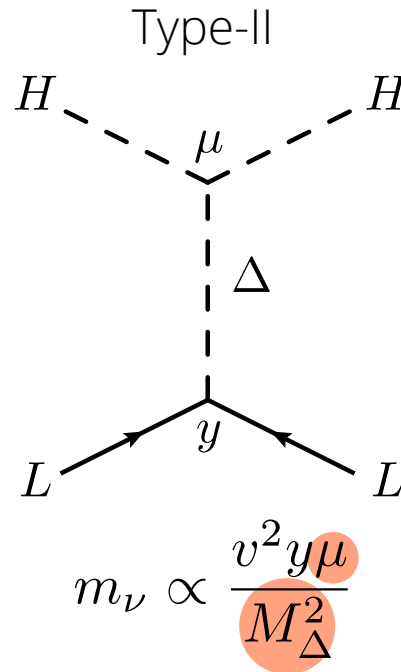
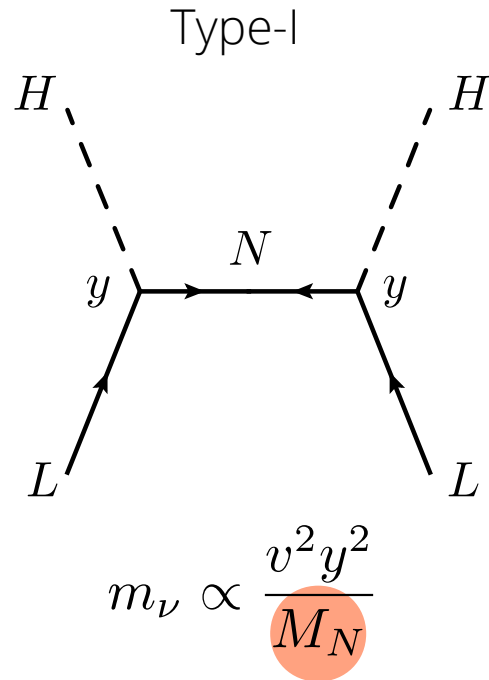
$$m_\nu \propto \frac{v^2 y \mu}{M_\Delta^2}$$



$$m_\nu \propto \frac{v^2 y^2}{M_\Sigma}$$

Neutrino mass mechanisms

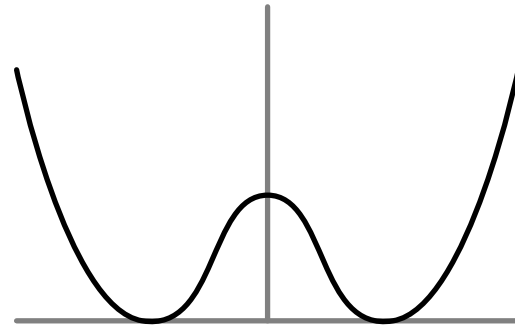
The commonly known schemes are **see-saw mechanisms**



Enters the Majoron

The Type-I seesaw can be generated by the **spontaneous** breaking of the **U(1) lepton number** symmetry

$$S = \frac{v_S + \sigma + iJ}{\sqrt{2}}$$

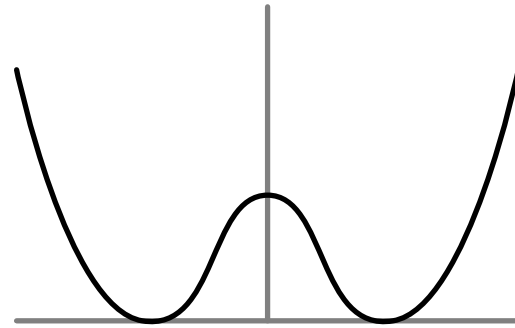


$$\mathcal{L} \supset -y_L \bar{L} H N^c - \frac{y_S}{2} S \bar{N}^c N + h.c.$$

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-1 0 1 2 -1 -1

Enters the Majoron

$$m_D = \frac{y_L v_H}{\sqrt{2}}$$

$$M_N = \frac{y_S v_S}{\sqrt{2}}$$

After the SSB, we get the Type-I seesaw

$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars: σ and J

$$m_\sigma \simeq v_S \quad m_J = 0$$

Enters the Majoron

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$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars: σ and J  DM candidate

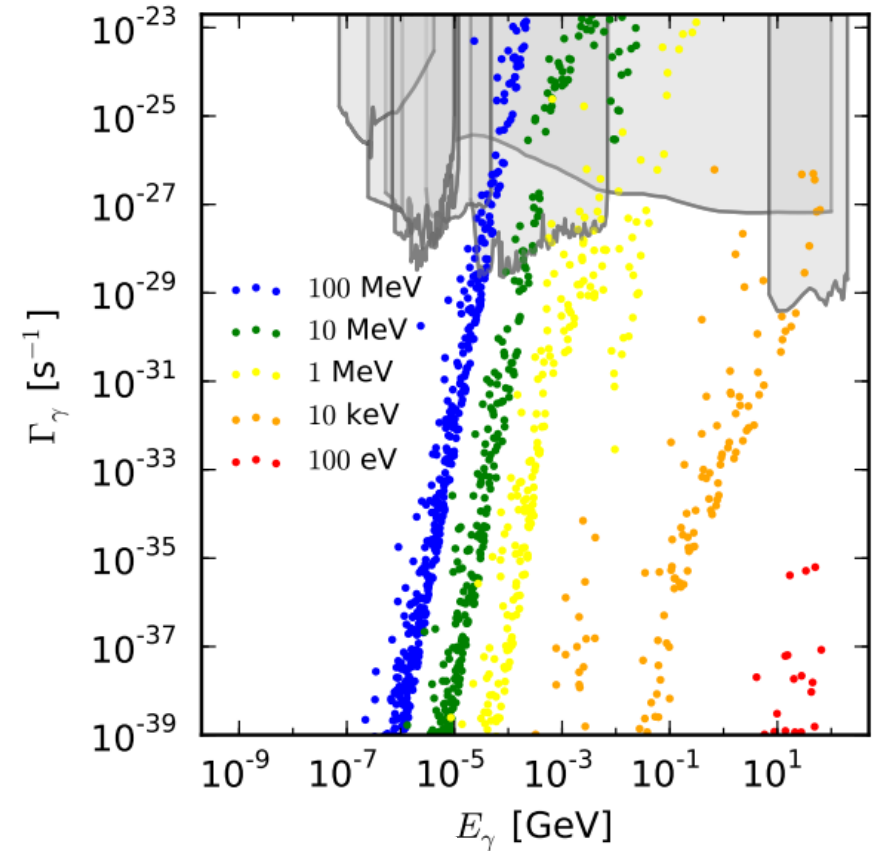
$$m_\sigma \simeq v_S \quad m_J = 0$$

Majoron as DM (pros)

- Neutral
- Weakly coupled to the SM
- Long lived

$$\Gamma_{J \rightarrow \nu\nu} = \frac{m_J}{32\pi} \frac{\sum_i (m_i^\nu)^2}{2v_1^2}$$

$$\Gamma_{J \rightarrow \gamma\gamma} = \frac{\alpha^2 m_J^3}{64\pi^3} \left| \sum_f N_f Q_f^2 \frac{2v_3^2}{v_2^2 v_1} (-2T_3^f) \frac{m_J^2}{12m_f^2} \right|^2$$



Details in arxiv: 1406.0004

Majoron as DM (cons)

$$m_J = 0 \quad ! ! ! !$$

... but global symmetries are not protected under gravity effects

Therefore

$$m_J \neq 0$$

... and the majoron DM is just a **pseudo Nambu-Goldstone boson**

Majoron as DM (our proposal)

ArXiv:1703.03416

What defines a **majoron DM**?

- It is a (pseudo)scalar
- It is part of the neutrino mass mechanism
- Its signature is the decay into neutrinos
- It is massive

Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

$$\mathcal{L} = -\frac{1}{2} n_L^T C \mathcal{M} n_L + h.c.$$

$$n_L^T = (\nu_L, N_1^c, N_2)$$

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

Inverse seesaw

The **standard** inverse seesaw

$$\mathcal{L} = -\frac{1}{2}n_L^T C \mathcal{M} n_L + h.c.$$

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$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

Lepton number
violating term



Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

Active neutrinos

$$m_\nu = \left(\frac{m_D}{M} \right)^2 \mu$$

Heavy neutrinos

$$m_{\mathcal{N}'} = M - \frac{m_D^2}{M} + \frac{\mu}{2}$$
$$m_{\mathcal{N}} = M - \frac{m_D^2}{M} - \frac{\mu}{2}$$

Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

Some numerology:

$$M \sim 100 \text{ TeV} \quad m_D \sim 10 \text{ GeV} \quad \mu \sim 10 \text{ MeV}$$

$$m_\nu \sim 0.1 \text{ eV}$$

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need to add **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$m_D = \frac{y_L v_h}{\sqrt{2}}, \quad M = \frac{y_S v_S}{\sqrt{2}}, \quad \text{and} \quad \mu = \frac{y_X v_X}{\sqrt{2}}$$

Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$v_S > 50 \text{ TeV} \quad v_X > 5 \text{ MeV}$$

Spontaneous Inverse seesaw

But the **charge assignments** do not follow the typical one of the ISS

	L	N_1	N_2	S	X
$SU(2)_L$	2	1	1	1	1
$U(1)_Y$	1/2	0	0	0	0
$U(1)_I$	1	-1	x	$1 - x$	$2x$

$$x = 3/5$$

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

Scalar potential

The **assignment** fixes the potential

$$\omega = \frac{v_X}{v_S}$$

$$V_{\text{scalar}} = V_{XS} + V_{HXS} + V_I$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X S^{\dagger 3} + h.c.$$

$$S = \frac{v_S e^{i\theta} + \sigma_S + i\chi_S}{\sqrt{2}}$$

$$X = \frac{v_X e^{i\tau} + \sigma_X + i\chi_X}{\sqrt{2}}$$

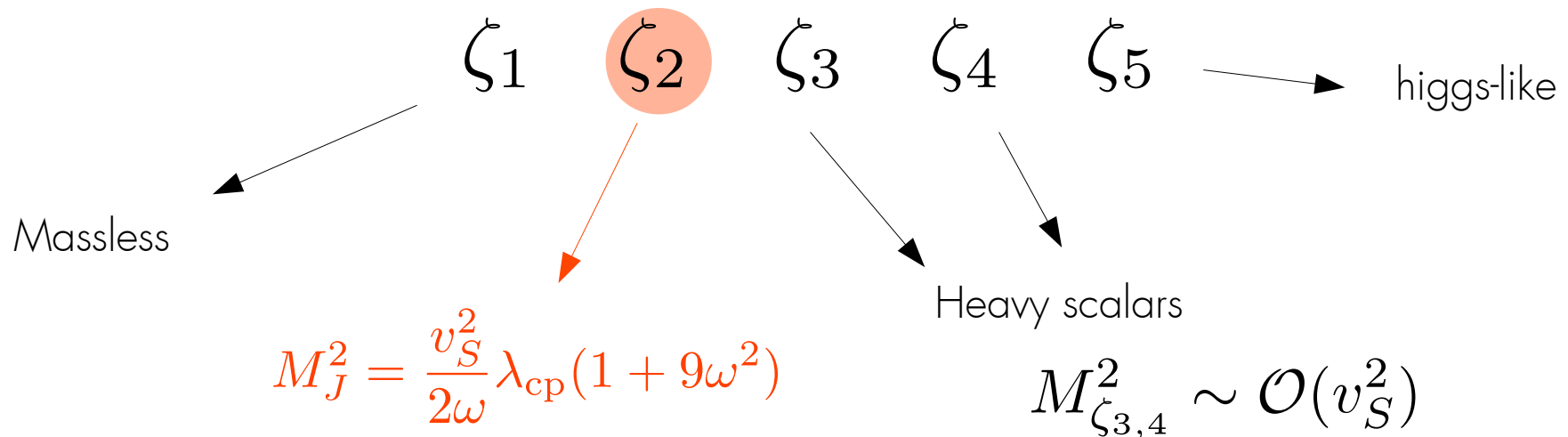
The tadpole equations relate the CP phases:

$$\tau = 3\theta - \delta - \pi$$

Mass spectrum

$$\omega = \frac{v_X}{v_S}$$

Now we have 5 spin-0 fields: 4 related to L breaking
1 related to EW breaking



Majoron DM stability

The only candidate is the **lightest massive scalar** i.e.

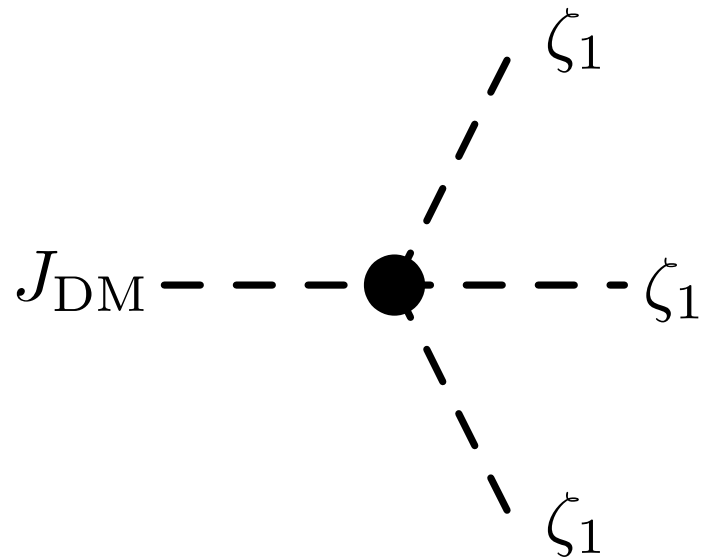
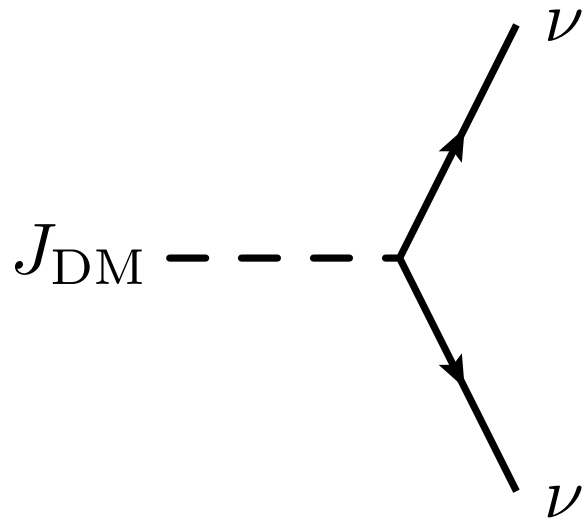
$$\zeta_2 = J_{\text{DM}}$$

We still has to satisfy the stability condition:

$$\Gamma_{\text{DM}} < 10^{-52} \text{ GeV}$$

Decay modes

There are potentially dangerous decay modes:



Decay into neutrinos

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

The decay rate vanishes for:

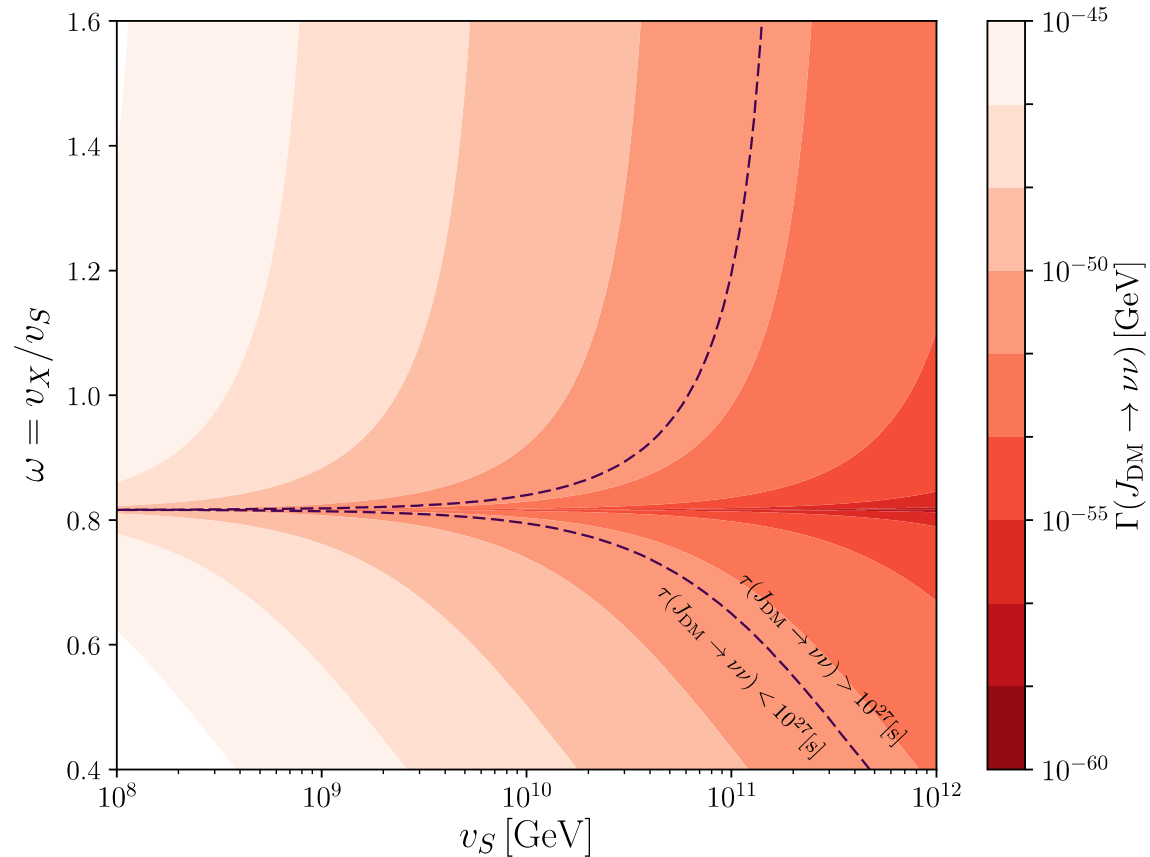
$$\omega_0 = \sqrt{2/3}$$

$$\Gamma_\nu = \Gamma_{0\nu}(\omega_0) 4\alpha^2$$

$$\Gamma_{0\nu}(\omega_0) \simeq 10^{-40} \text{ GeV} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^2 \left(\frac{M_J}{1 \text{ keV}} \right) \left(\frac{v_S}{100 \text{ TeV}} \right)^{-2}$$

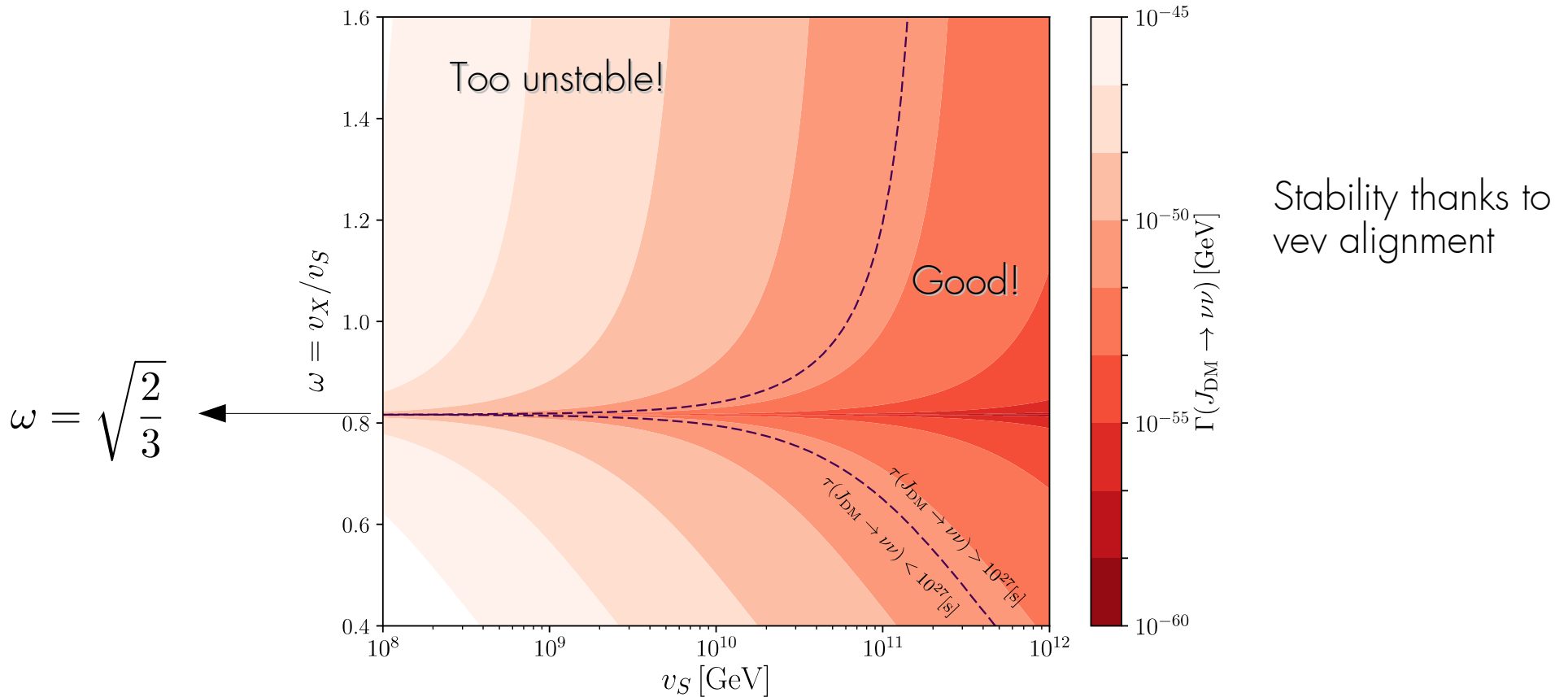
Decay into neutrinos

$$J_{\text{DM}} \rightarrow \nu\nu$$



Decay into neutrinos

$$J_{\text{DM}} \rightarrow \nu\nu$$



Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$

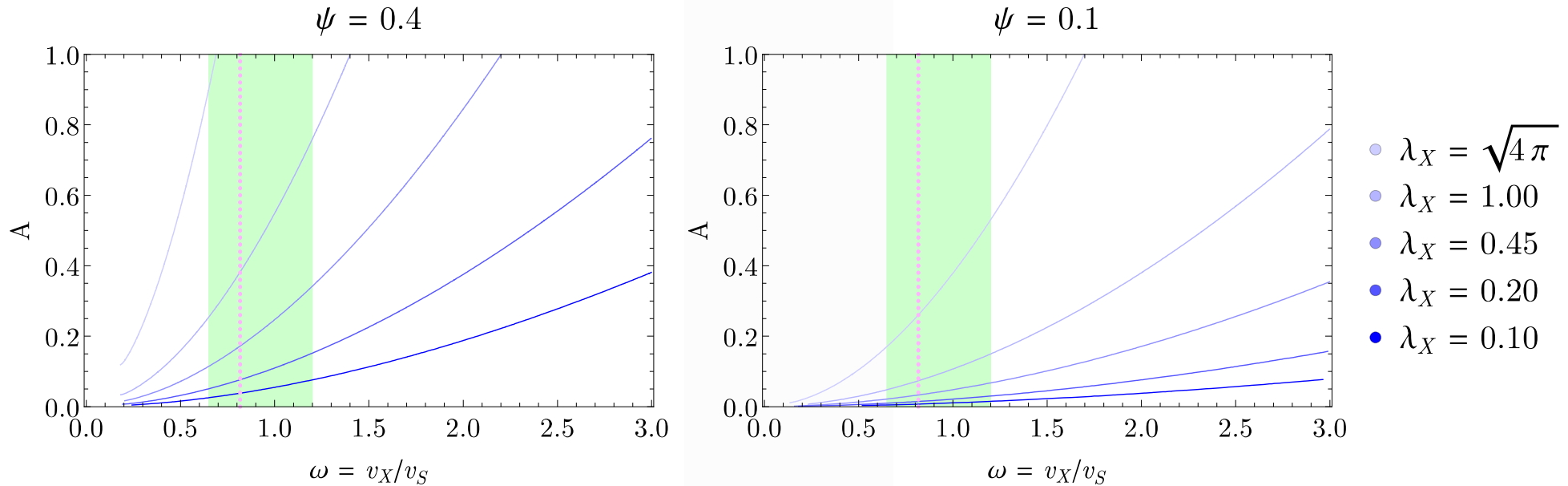
Without a protective symmetry, this channel is not suppressed

However we can find the parameter space where the **mode vanishes**

$$J_{\text{DM}} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_1 \\ \searrow \zeta_1 \end{array} \lambda_{2111}^{\text{eff}} = J_{\text{DM}} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_1 \\ \searrow \zeta_1 \end{array} \lambda_{2111} + \sum_{k=3,4,5} J_{\text{DM}} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_k \\ \searrow \zeta_1 \end{array} \lambda_{12k} \lambda_{11k}$$

Decay into scalars

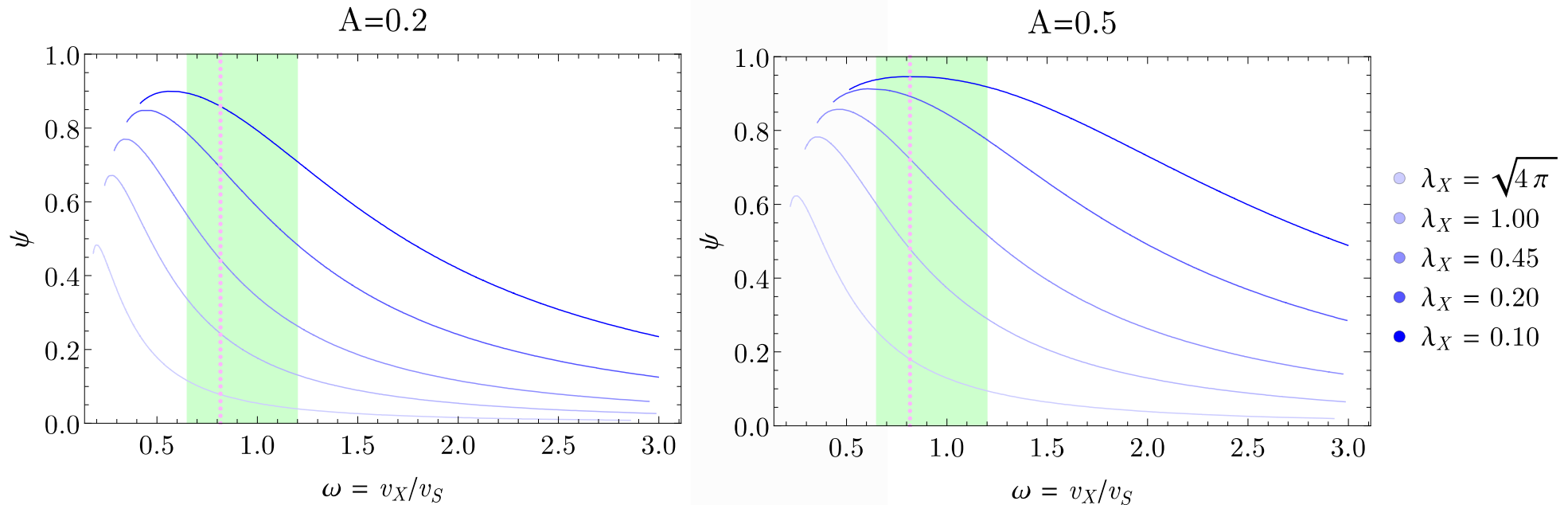
$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



The interplay of different diagrams allows to vanish the decay mode

Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



There is a whole volume that satisfy this condition

Conclusions (of this part)

- The **spontaneous inverse seesaw** provides a well suited majoron DM candidate
- Our **majoron DM** is phenomenologically equivalent to the PNGB
- The **vev alignment** has a relevant role in the DM stability

Example 2

Dark Matter interaction
with neutrinos

Neutrino oscillations

Flavor and mass eigenstates **do not coincide** $|\nu_\alpha\rangle = \sum_k U_{\alpha k}^* |\nu_k\rangle$

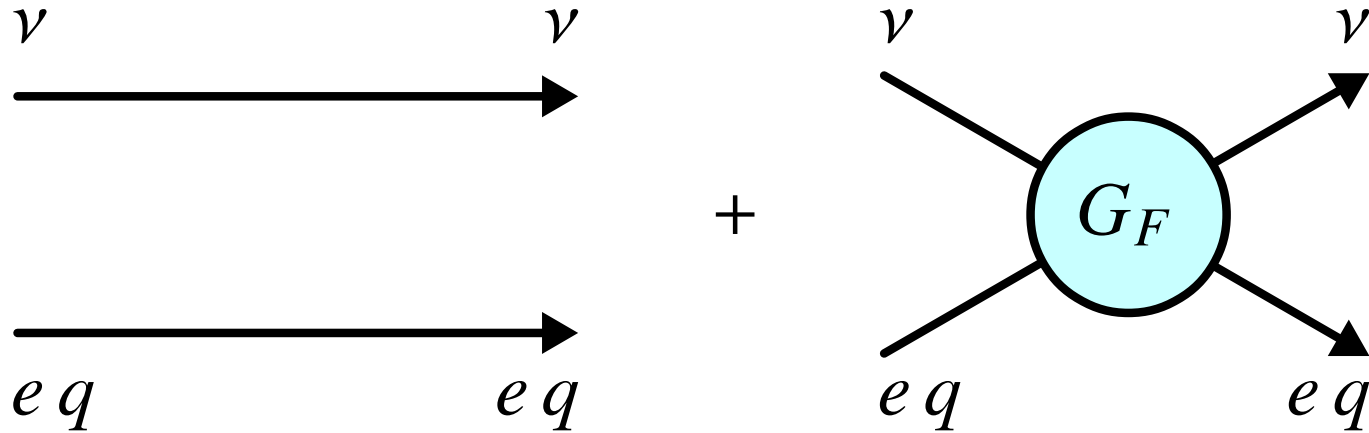
Mass eigenstates
evolve according to:

$$i \frac{\partial \Psi}{\partial t} = \mathcal{H} \Psi$$
$$\mathcal{H}_{\text{vac}} = \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger$$

The final ν flavor depends on: **Initial state, Source distance, Neutrino energy**

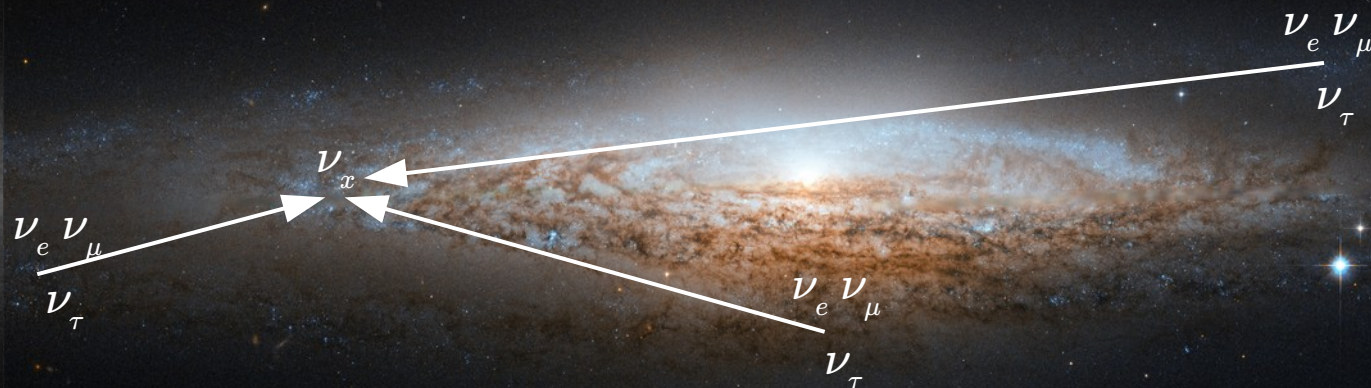
Matter effects (a.k.a. MSW effect)

The interaction with a medium modifies the oscillation patterns w.r.t. vacuum



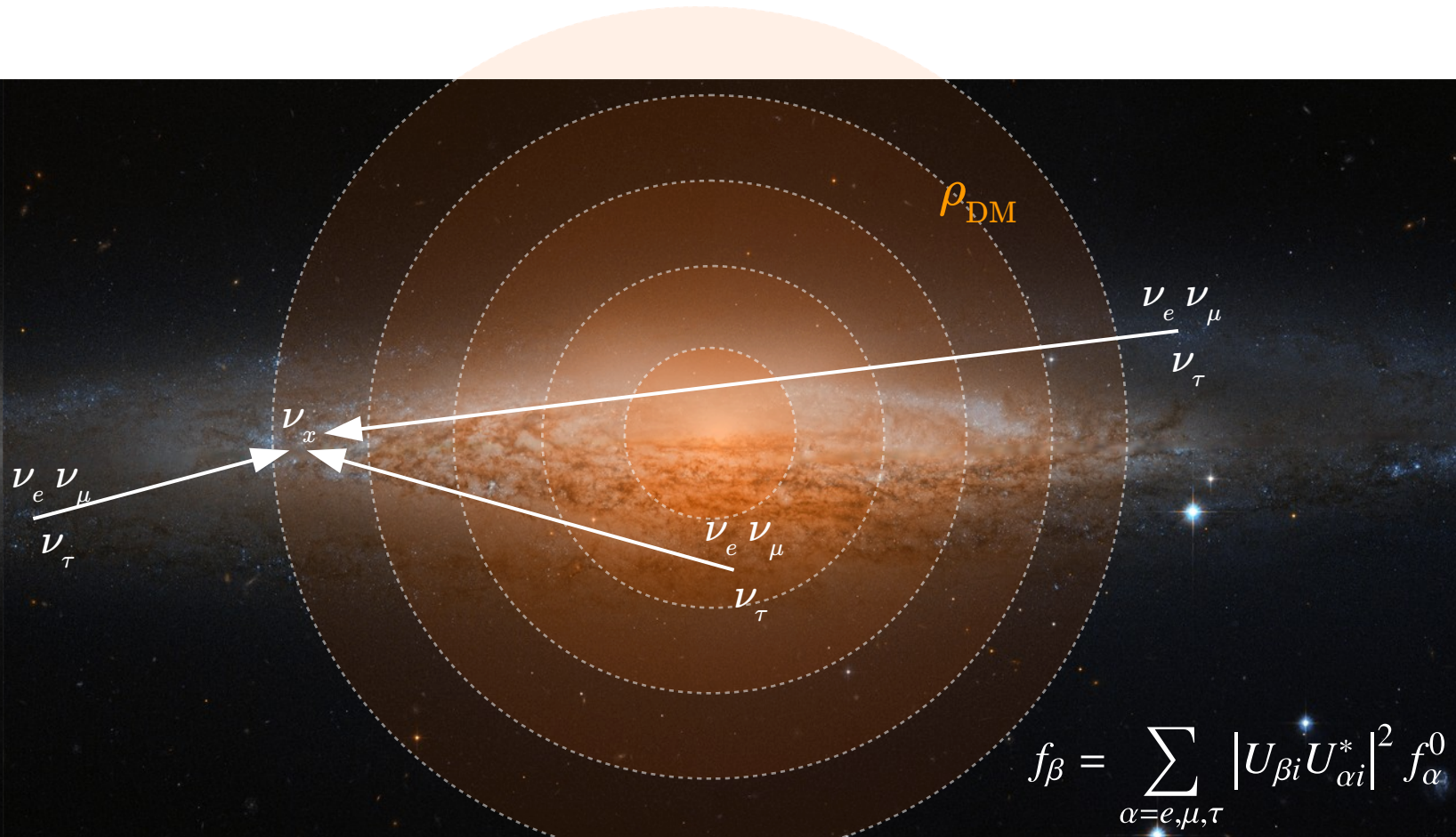
$$\mathcal{H}_{\text{tot}} = \mathcal{H}_{\text{vac}} + \mathcal{V}$$

Dark Matter effects

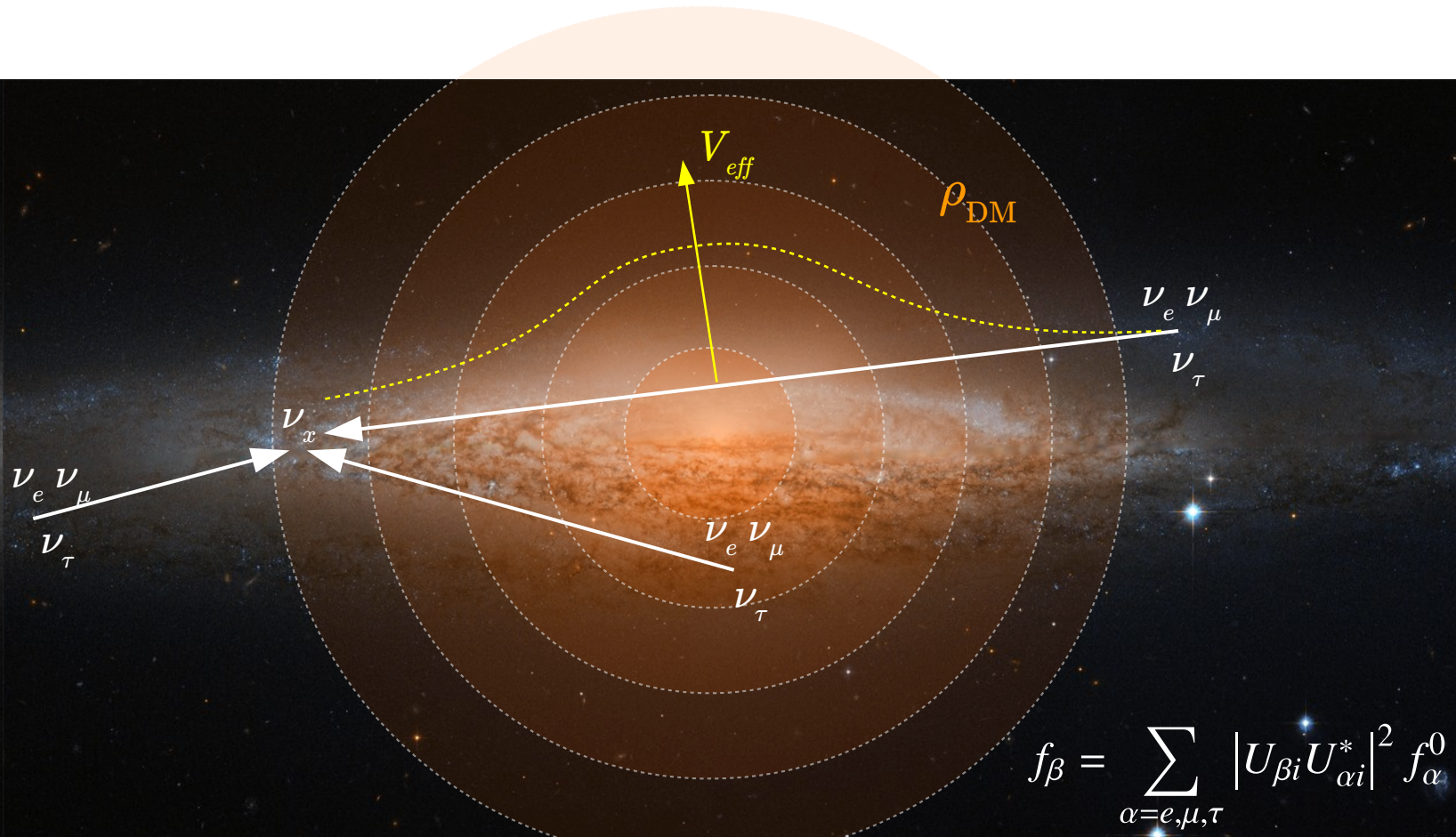


$$f_\beta = \sum_{\alpha=e,\mu,\tau} |U_{\beta i} U_{\alpha i}^*|^2 f_\alpha^0$$

Dark Matter effects



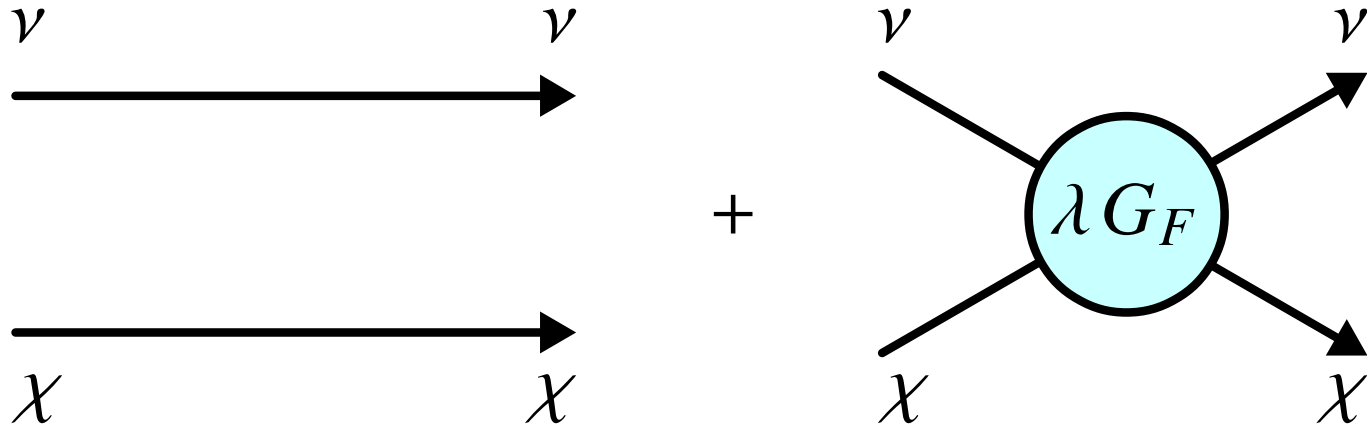
Dark Matter effects



$$f_{\beta} = \sum_{\alpha=e,\mu,\tau} |U_{\beta i} U_{\alpha i}^*|^2 f_{\alpha}^0$$

Dark Matter effects

The interaction with DM might modify the oscillation patterns w.r.t. vacuum



$$\mathcal{H}_{\text{tot}} = \mathcal{H}_{\text{vac}} + \mathcal{V}$$

Dark Matter effects

We parameterized the effective potential using a “weak interaction” form:

$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

But also spatial dependency:

$$\mathcal{V}_{\alpha\beta} = \mathcal{V}_{\alpha\beta}^\oplus \times f_{\text{DM}}(r)$$

Dark Matter effects

We parameterized the effective potential using a “weak interaction” form:

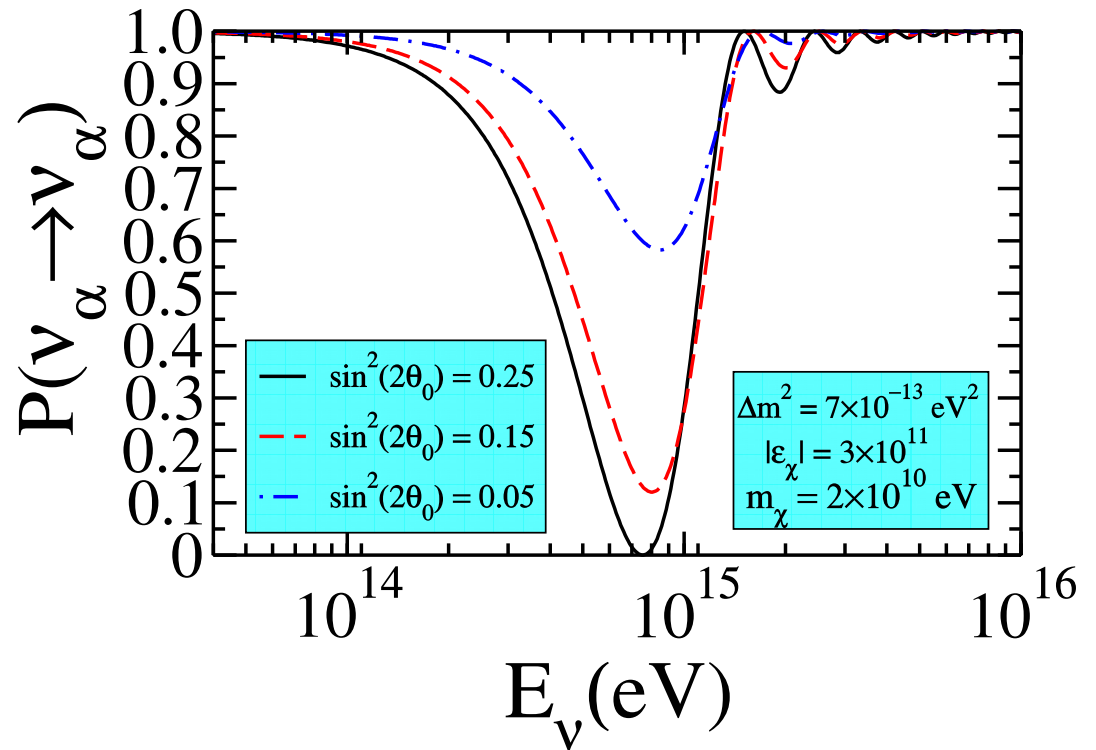
$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

But also spatial dependency:


$$\mathcal{V}_{\alpha\beta} = \mathcal{V}_{\alpha\beta}^\oplus \times f_{\text{DM}}(r)$$

Dark Matter effects (1 + 1) neutrinos

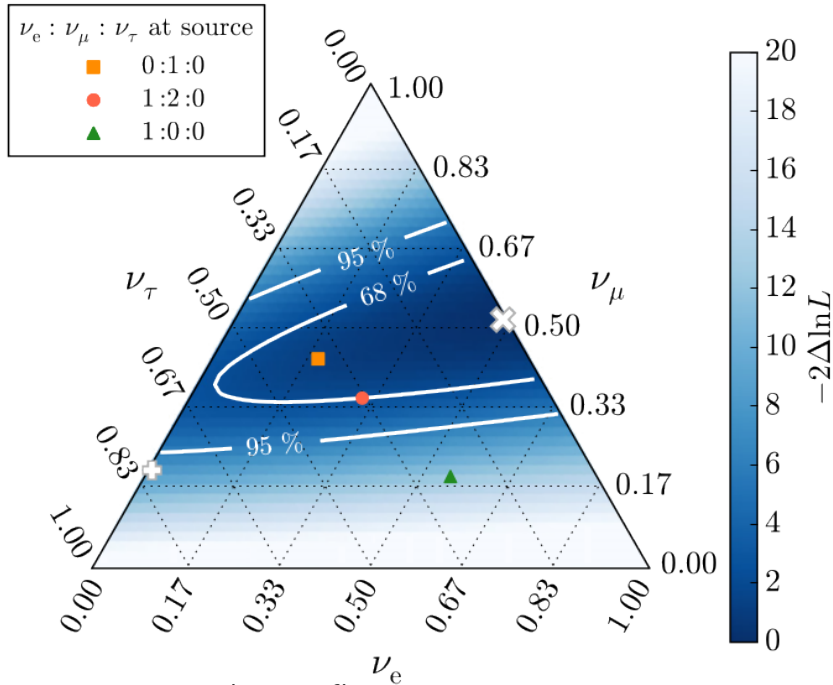
The effect in the neutrino oscillation due to DM was studied showing that **resonances** maybe important



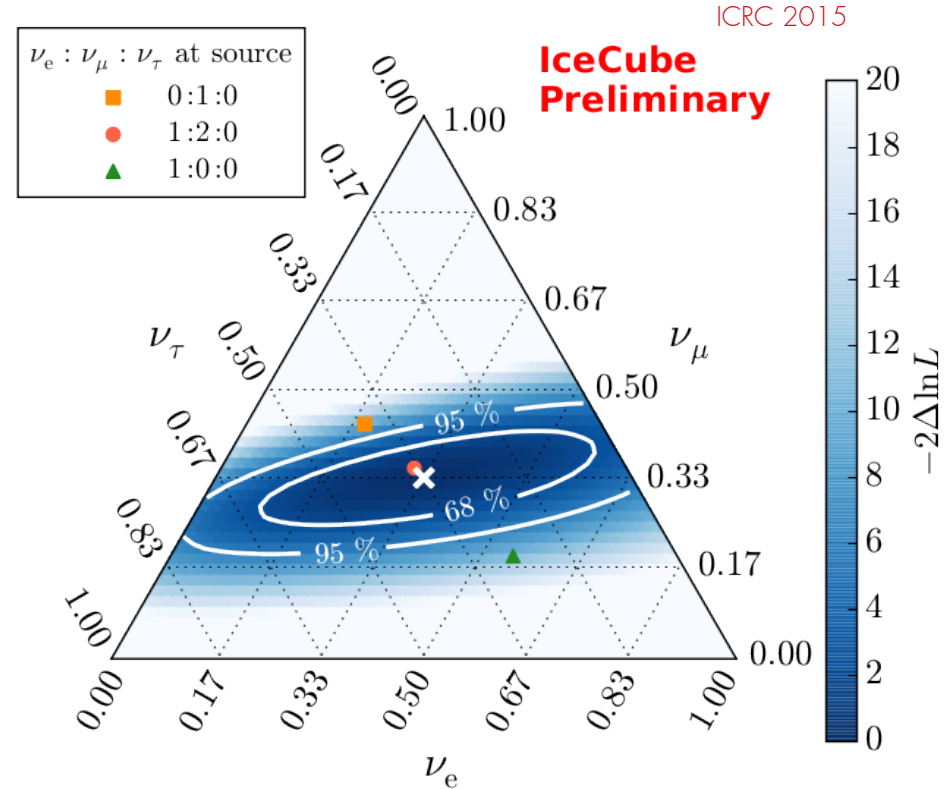
Mixing angle and mass splitting are free

Flavor composition in IceCube

THE ASTROPHYSICAL JOURNAL, 809:98 (15pp), 2015 August 10

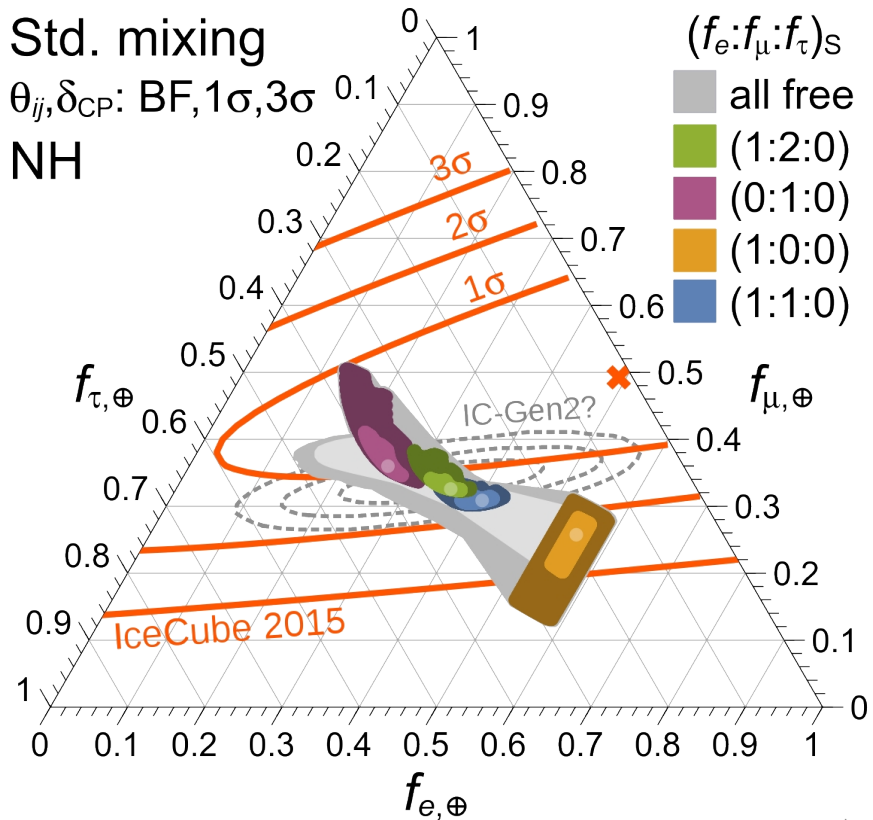


Latest result on flavor composition

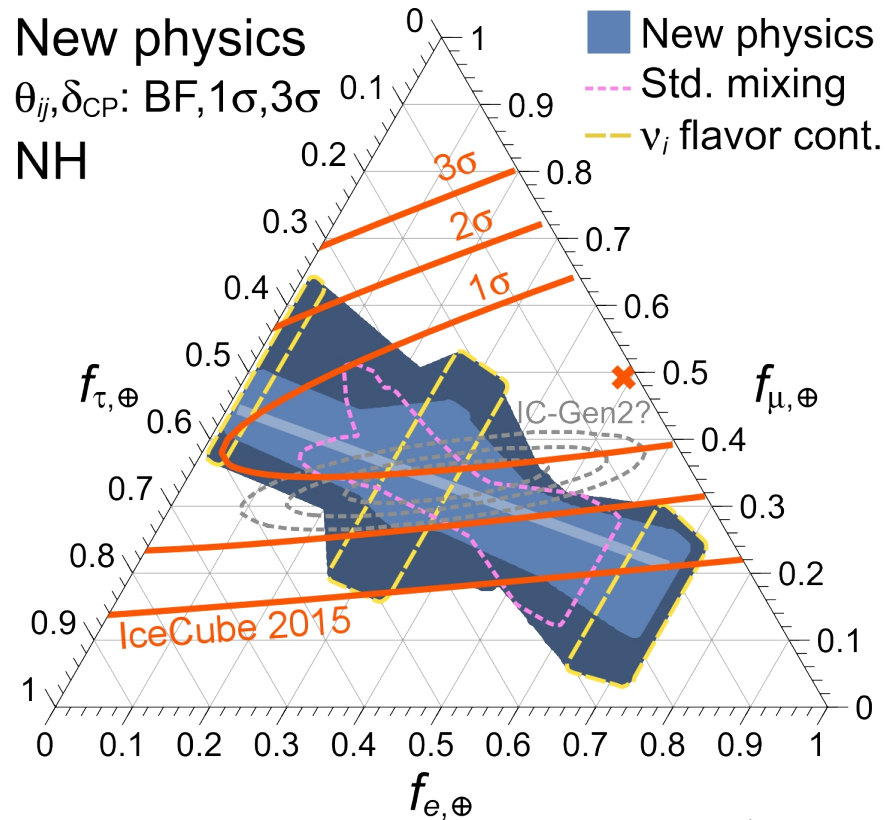


Sensitivity after 10 years

What we expect?

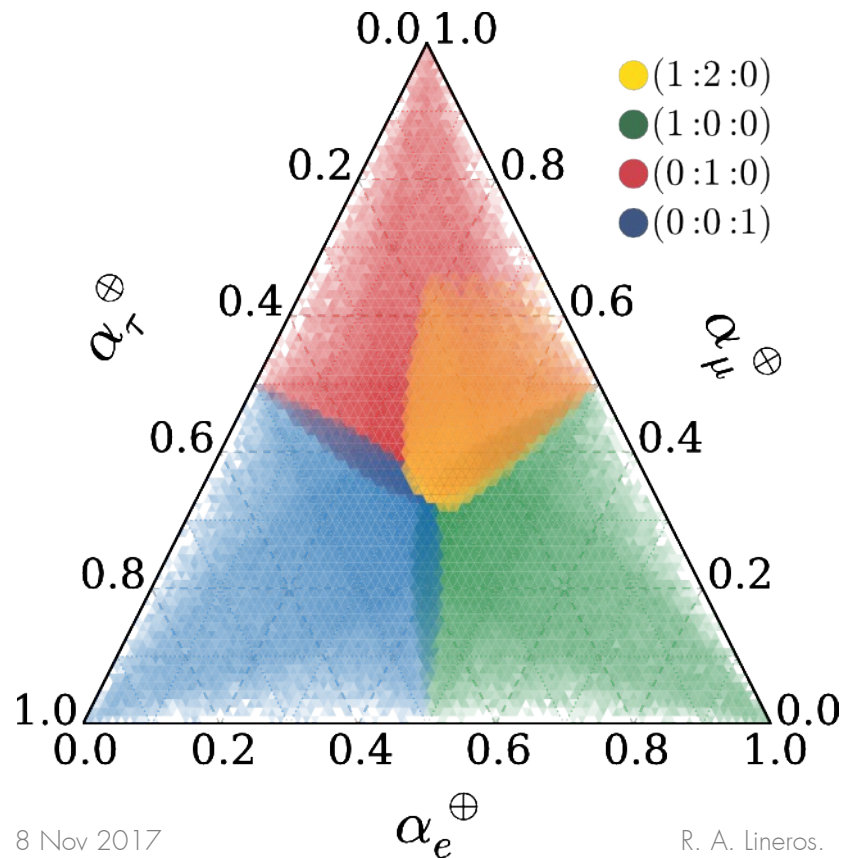


M. Bustamante et al. PRL 115, 161302 (2015)



Effects from New Physics

Argüelles et al. PRL 115, 161303 (2015)

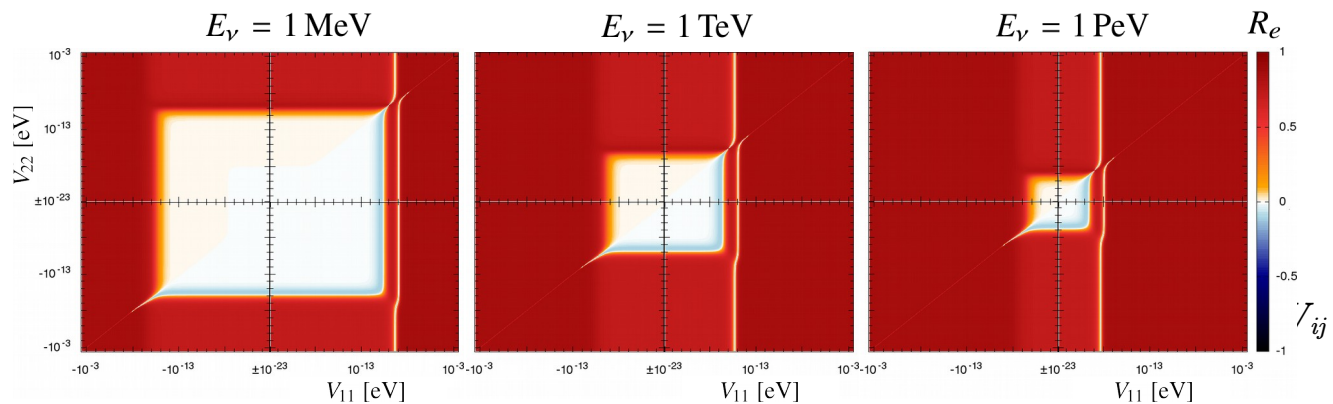


Sources of New Physics:

- Space torsion
- CPT - Lorentz violation

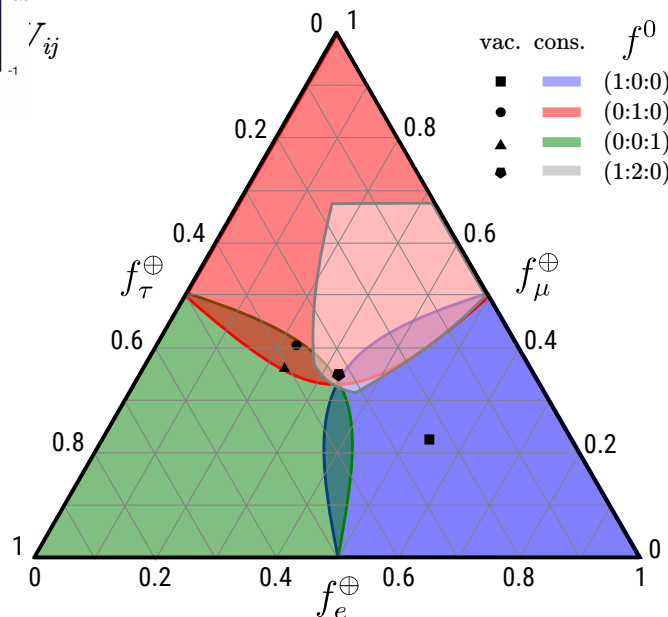
All NP effects are **homogeneous** in space

Composition in a homogeneous halo



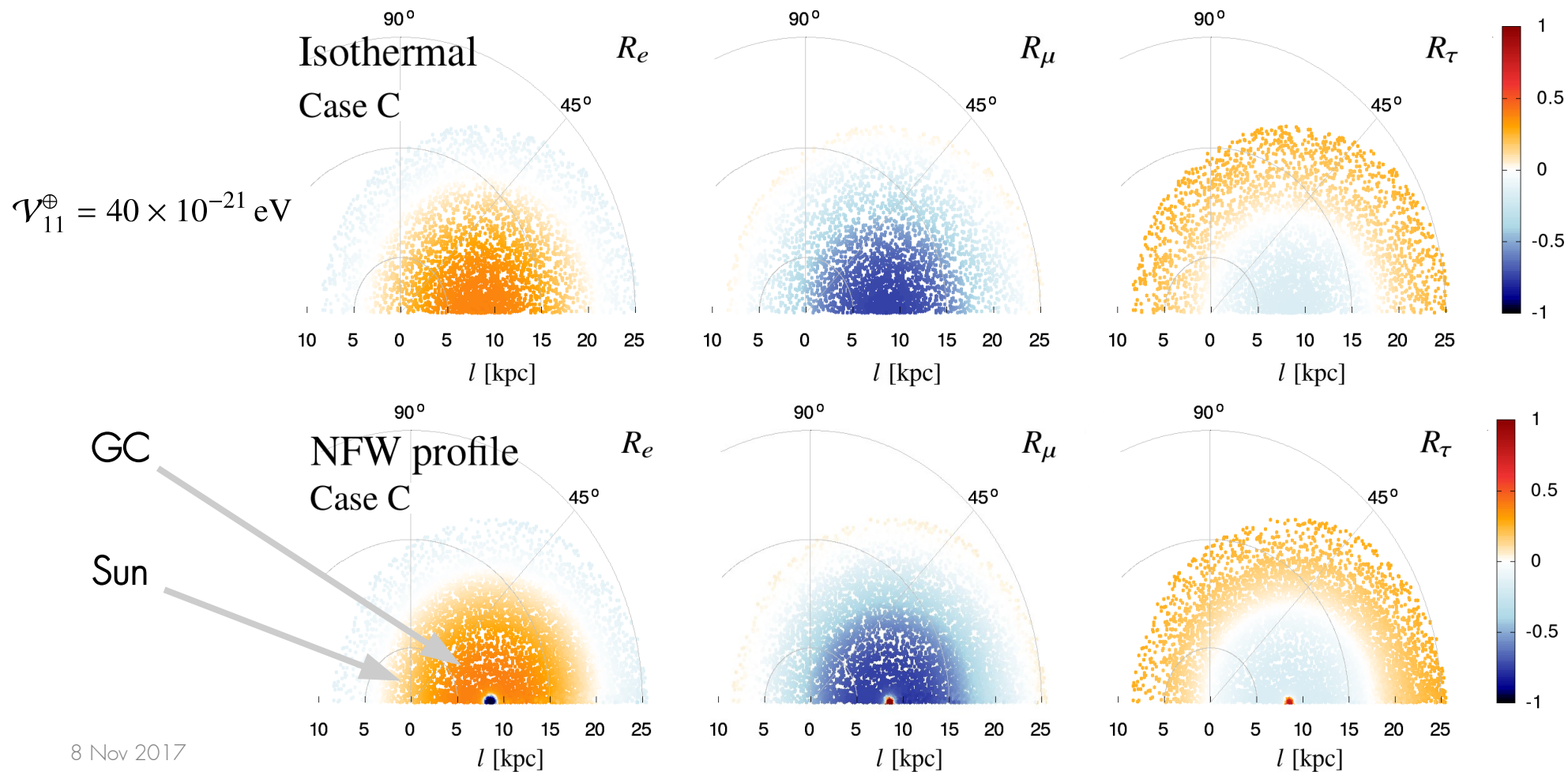
Homogeneous DM distribution can mimic
New Physics effects

Higher ν -energy, smaller potential are
accessible

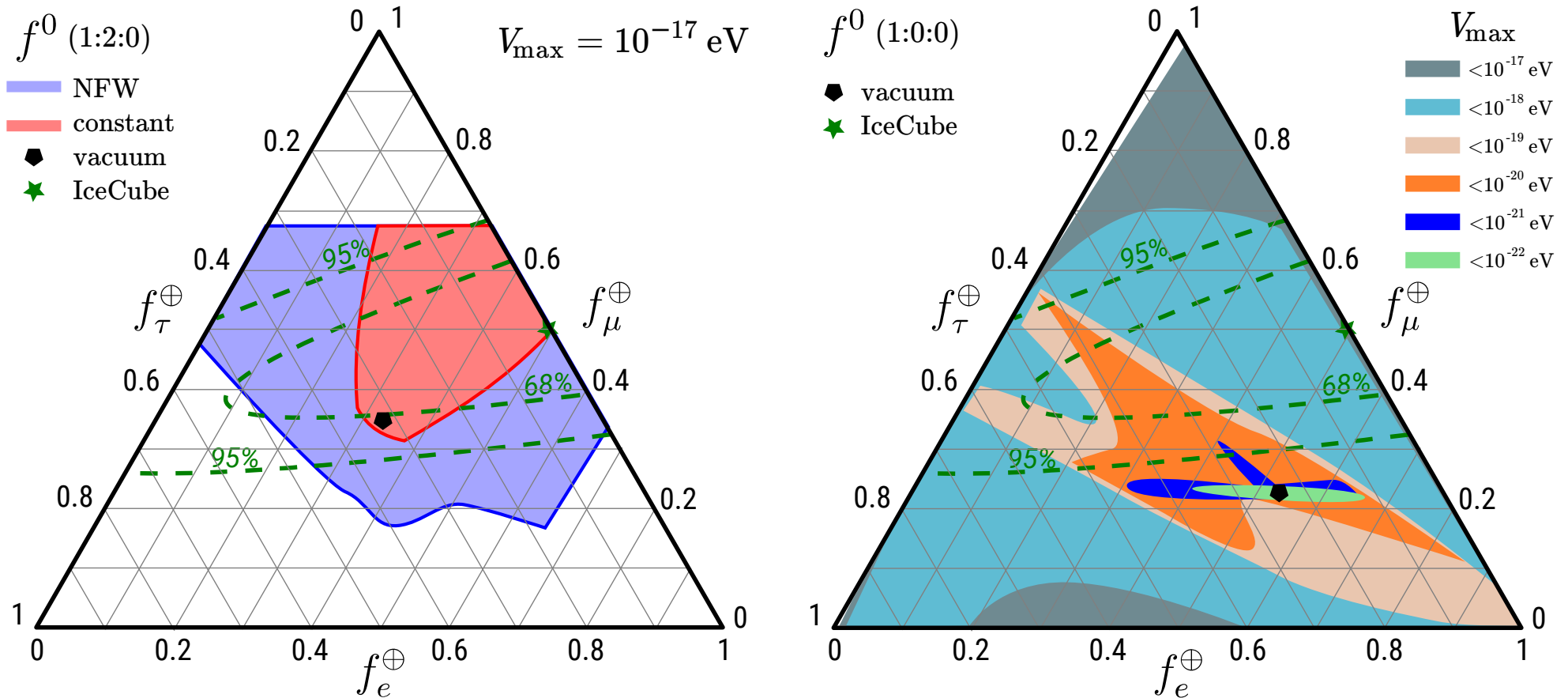


Spatial dependence

$$\mathcal{V}_{\alpha\beta} = \mathcal{V}_{\alpha\beta}^{\oplus} \times f_{\text{DM}}(r)$$

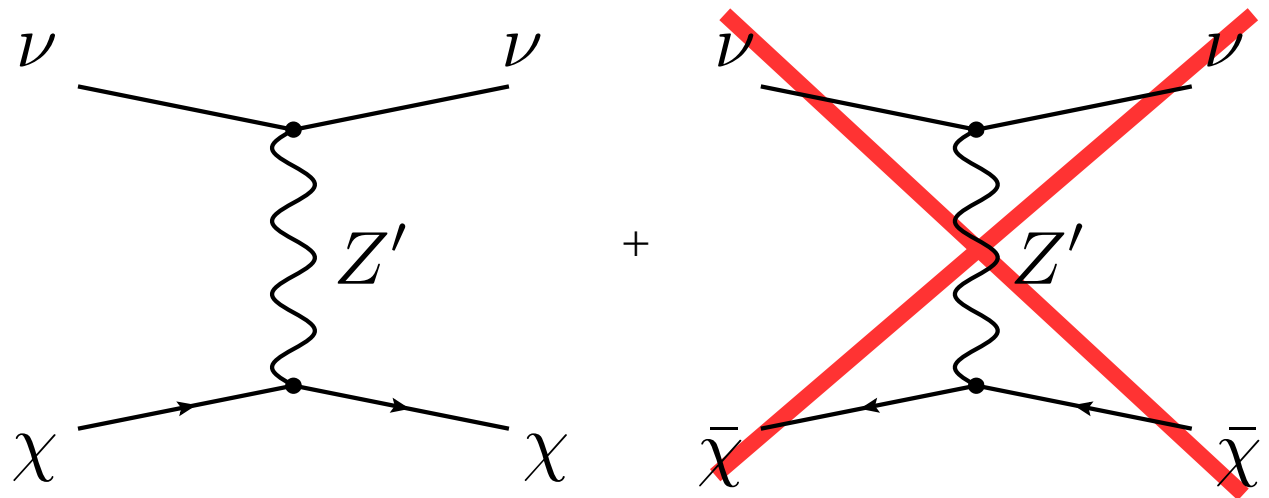
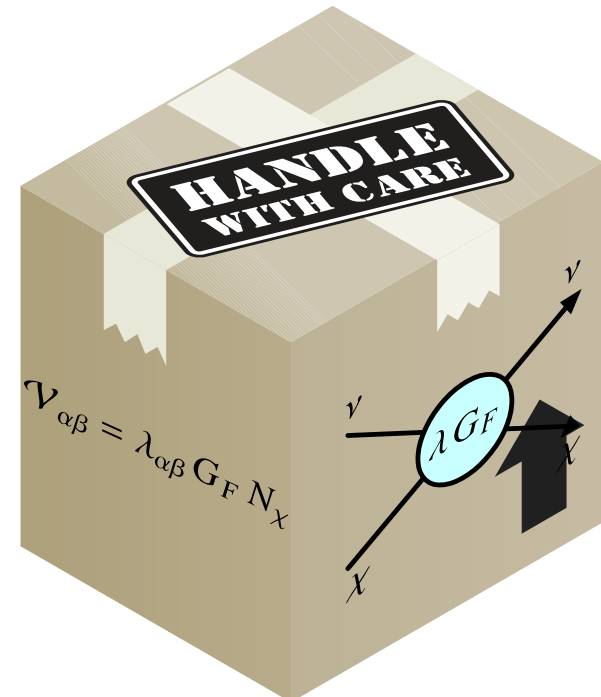


Composition in a NFW halo



Particle physics interpretation

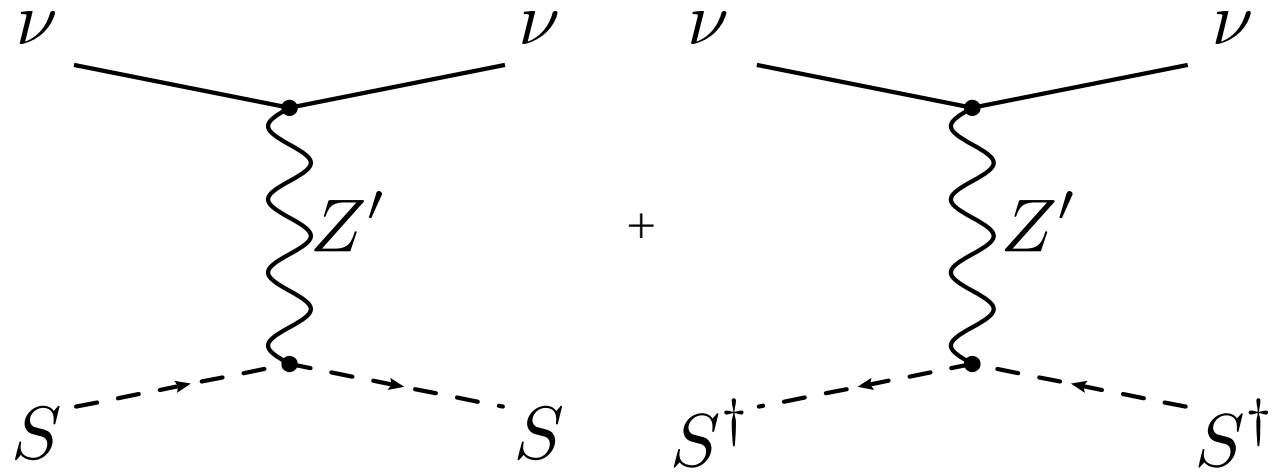
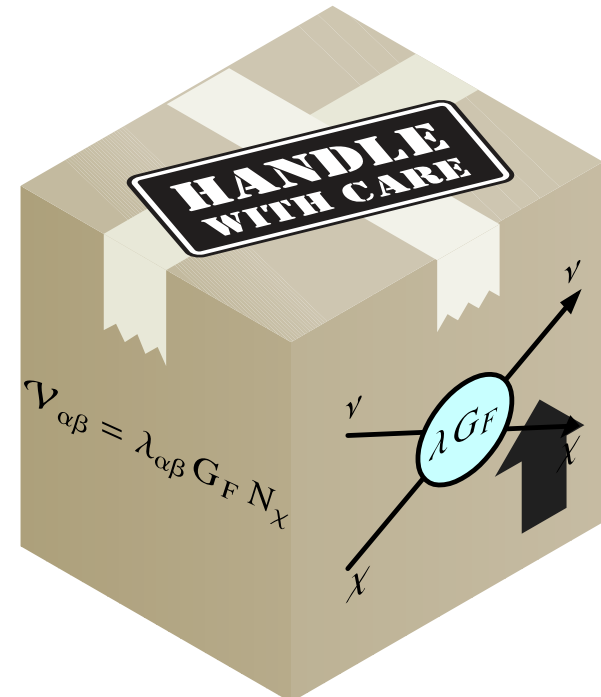
The simplest scenarios are models with asymmetric DM



$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

Particle physics interpretation

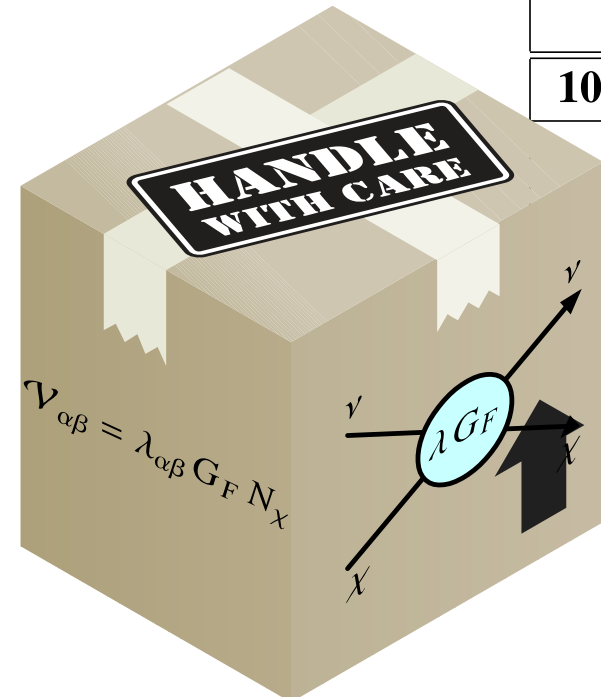
Or with scalar DM



$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

Particle physics interpretation

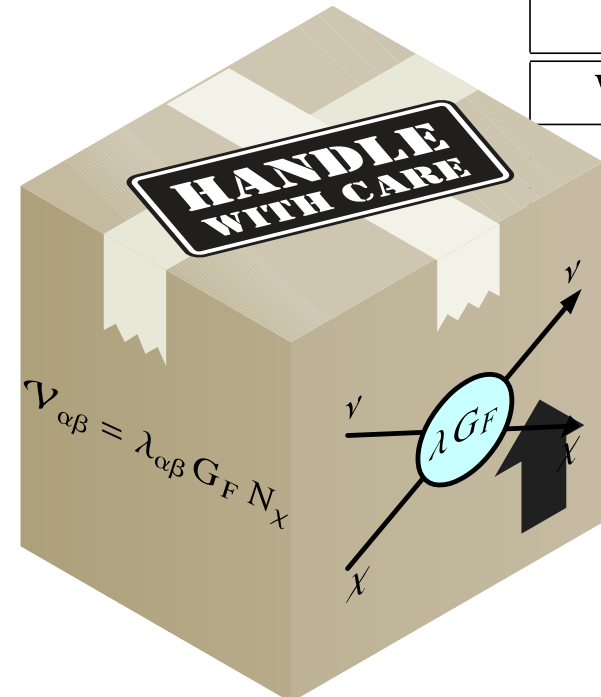
V_{11}^{\oplus} [eV]	10^{-21}	10^{-19}	10^{-17}
Weak scale (a) assumptions: $G'_F = G_F, \lambda_{11} = 1$			
m_{DM} [eV]	10^{-8}	10^{-10}	10^{-12}
l_{ν} [pc]	10^{-2}	10^{-4}	10^{-6}
100 GeV DM (a) assumptions: $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^{-2}	10^{-4}	10^{-6}
1 keV DM (a) assumptions: $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^2	1	10^{-2}



One can try to explain the effective potential in terms of **particle physics scales**

Particle physics interpretation

V_{11}^{\oplus} [eV]	10^{-21}	10^{-19}	10^{-17}
Weak scale (a) assumptions: $G'_F = G_F, \lambda_{11} = 1$			
m_{DM} [eV]	10^{-8}	10^{-10}	10^{-12}
l_{ν} [pc]	10^{-2}	10^{-4}	10^{-6}
Weak scale (b) assumptions: $G'_F = G_F, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
m_{DM} [eV]	10^{-15}	10^{-19}	10^{-23}

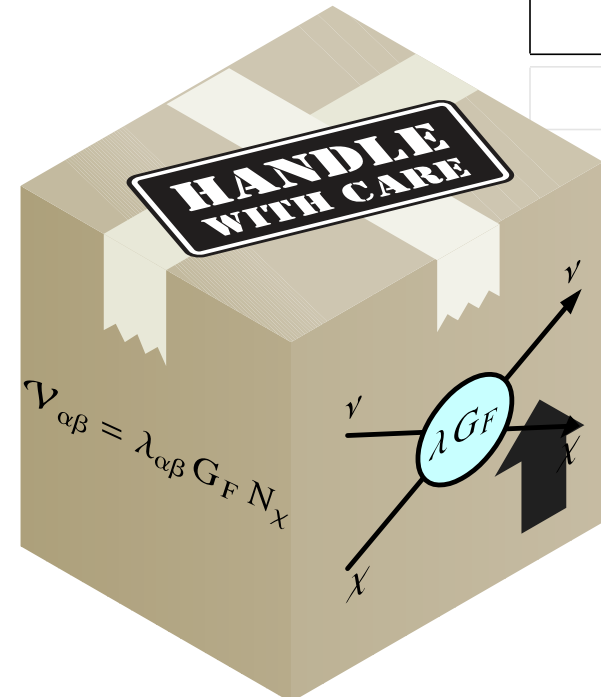


Assuming **weak scale** couplings and mediators DM has to be **extremely light**. Fuzzy DM, Bose-Einstein DM?

For $\lambda=1$, the mean free path is sub-pc :-|

Particle physics interpretation

V_{11}^{\oplus} [eV]	10^{-21}	10^{-19}	10^{-17}
100 GeV DM (a) assumptions: $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^{-2}	10^{-4}	10^{-6}
1 keV DM (a) assumptions: $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^2	1	10^{-2}



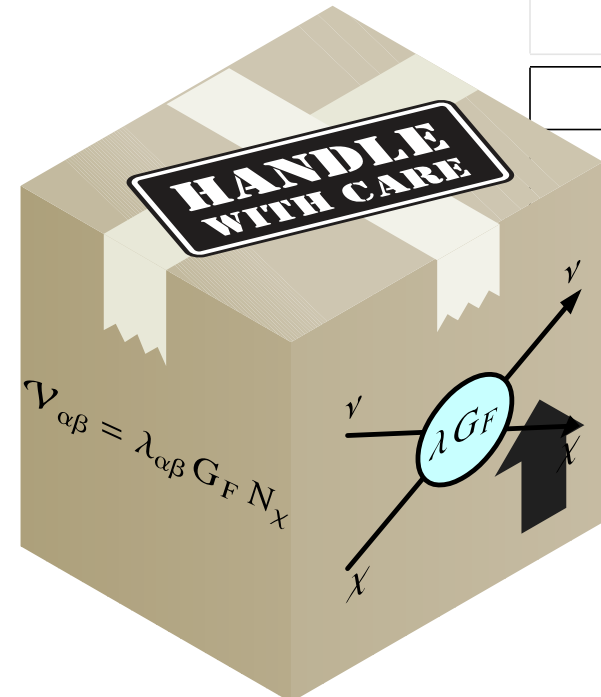
100 GeV DM

sub-eV mediators, $g \sim \lambda^{1/2} = 10^{-3} - 10^{-6}$

$$\sigma_{\nu\chi} = 1.62 \times 10^{-23} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

Particle physics interpretation

V_{11}^{\oplus} [eV]	10^{-21}	10^{-19}	10^{-17}
100 GeV DM (a) assumptions: $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^{-2}	10^{-4}	10^{-6}
1 keV DM (a) assumptions: $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 50 \text{ kpc}$			
λ_{11}	10^{-7}	10^{-9}	10^{-11}
$m_{Z'}$ [eV]	10^2	1	10^{-2}



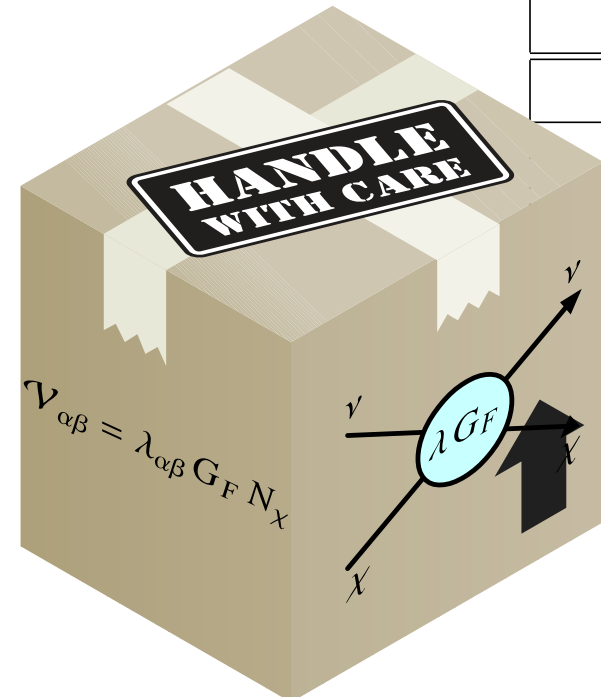
1 keV DM

eV mediators, $g \sim \lambda^{1/2} = 10^{-3} - 10^{-6}$

$$\sigma_{\nu\chi} = 1.62 \times 10^{-23} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

Particle physics interpretation

V_{11}^{\oplus} [eV]	10^{-21}	10^{-19}	10^{-17}
100 GeV DM (b) assumptions: $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 10^6 \text{ Gpc}$			
λ_{11}	10^{-17}	10^{-19}	10^{-21}
$m_{Z'}$ [eV]	10^{-7}	10^{-9}	10^{-11}
1 keV DM (b) assumptions: $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 10^6 \text{ Gpc}$			
λ_{11}	10^{-17}	10^{-19}	10^{-21}
$m_{Z'}$ [eV]	10^{-3}	10^{-5}	10^{-7}



Assuming mean free path larger than the **Observable Universe**

Wilkinson et al. JCAP 1405 (2014) 011

$$\sigma_{\nu\chi} = 10^{-33} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

@MeV!

Conclusions (of this part)

- Flavor composition might open a door to **New-Physics** effects
- Effects from the **DM halo** modify the **oscillation pattern** differently than in the homogeneous scenario
- (Hopefully) **Correlation** between flavor and arrival direction might serve as test of this hypothesis
- A particle physics explanation requires mediators lighter than **eV**

Final words

- Neutrinos observables and DM are keys to unveil New Physics
- DM candidates lighter than WIMPs can affect neutrino observables
- We need to propose new way to test «unobservable» DM candidates

Dark Matter Hunters

Digital resources for hunting the dark sector

dmhunters.org

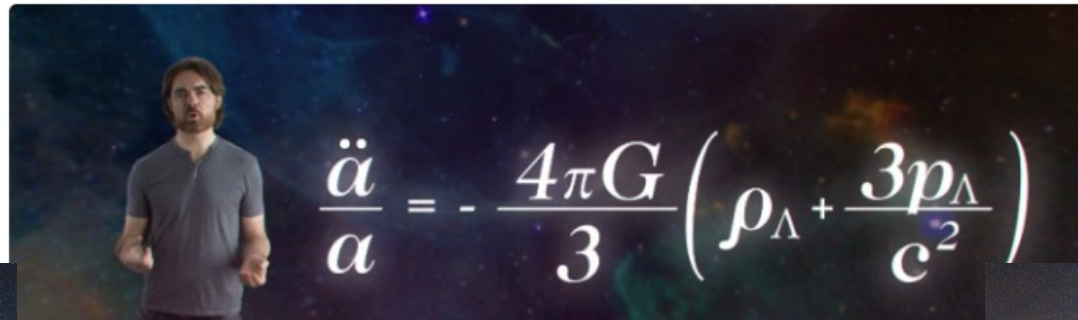
FOLLOW:



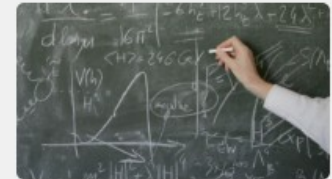
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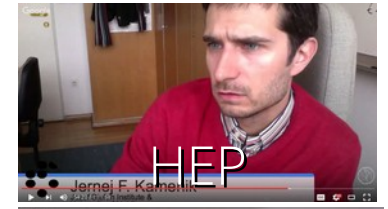
Latin American Webinars on Physics

**Sum Rules for
Flavour Parameters**

Martin Spinrath, NCTS (Taiwan)

Host: Joel Jones
Wednesday 3 May 2017 15:00 UTC

09:00 Colorado - 10:00 Mexico City, Lima, Bogotá - 11:00 New York - 12:00 Santiago, São Paulo, Buenos Aires - 16:00 London - 17:00 Brussels



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 lawphysics.wordpress.com

Thanks

Backup

Charge assignments

5 possible models

	L	N_1	N_2	S	X
$n = 1$	1	-1	1/7	6/7	2/7
$n = 2$	1	-1	1/3	2/3	2/3
$n = 3$	1	-1	3/5	2/5	6/5

$$m+n = 4$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X^m S^{\dagger n}$$

$$m+n = 3$$

	L	N_1	N_2	S	X
$n = 1$	1	-1	1/5	4/5	2/5
$n = 2$	1	-1	1/2	1/2	1

The rest of the scalar potential

$$V_{SX} = -\mu_S^2 |S|^2 + \frac{\lambda_S}{4} |S|^4 - \mu_X^2 |X|^2 + \frac{\lambda_X}{4} |X|^4 + \lambda_5 |S|^2 |X|^2 + V_I$$

$$V_{HSX} = -\mu_H^2 H^\dagger H + \frac{\lambda_H}{4} (H^\dagger H)^2 + \lambda_{HS} |S|^2 H^\dagger H + \lambda_{HX} |X|^2 H^\dagger H$$

Mass spectrum

$$m_h^2 \simeq \frac{v_h^2}{2} \left\{ \frac{\lambda_H}{2} + 2 \left(\frac{\lambda_{HX}^2 \lambda_S + \lambda_{HS}^2 \lambda_X - 4\lambda_5 \lambda_{HS} \lambda_{HX}}{4\lambda_5^2 - \lambda_S \lambda_X} \right) \right\}$$

$$M_{\zeta_3}^2 \simeq \frac{v_S^2}{2} \left(\frac{-A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$M_{\zeta_4}^2 \simeq \frac{v_S^2}{2} \left(\frac{A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$\lambda_S = A + \lambda_X \omega^2$$

$$\lambda_5 = -A \left(\frac{\sqrt{1 - \psi^2}}{4\omega\psi} \right)$$

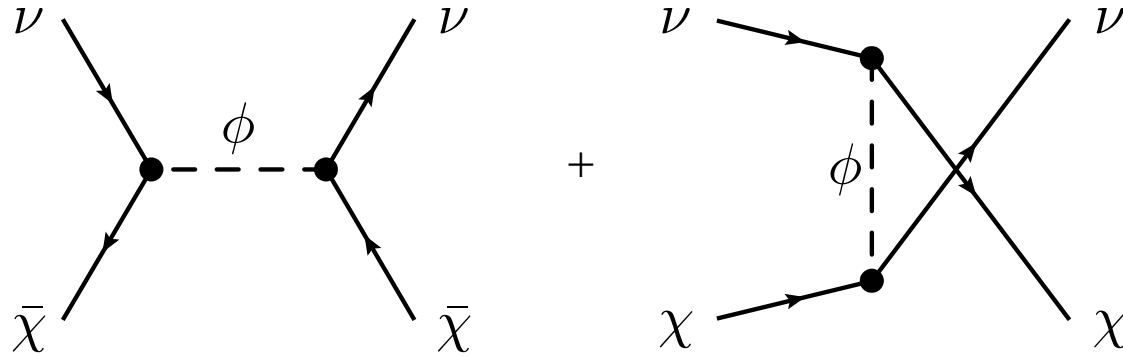
Numerology

Parameter	Value
M	100 TeV
μ	10 MeV
m_D	10 GeV
v_S	$10^8 - 10^{12}$ GeV
ω	0.4 - 1.6

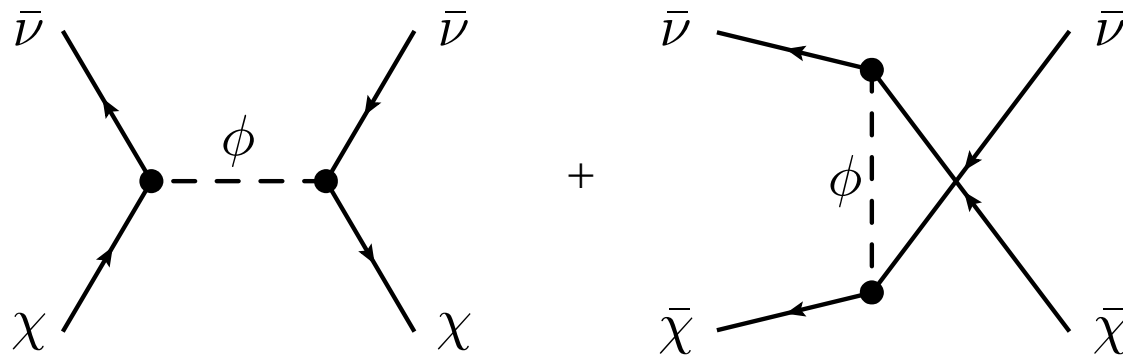
$$\lambda_{\text{cp}} \simeq \frac{M_J^2}{v_S^2} < 10^{-22}$$

Dirac DM model

Neutrinos



Antineutrinos



No cancellation at first order due to diagrams are different