



lawphysics  
Latin American Webinars on Physics

# Crash course on tools for Dark Matter research

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Dark Matter Days 2017 – CIFFU BUAP

# Motivation

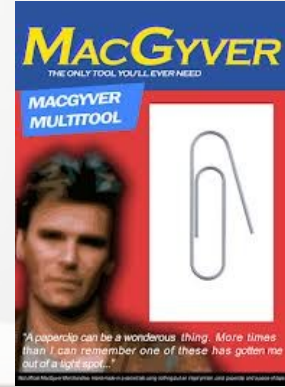
Research on Dark Matter  
could be hard without  
a good set tools



disclaimer: I don't know who is this guy

# Motivation

We hope for a unique tool to solve all our problems (in physics)

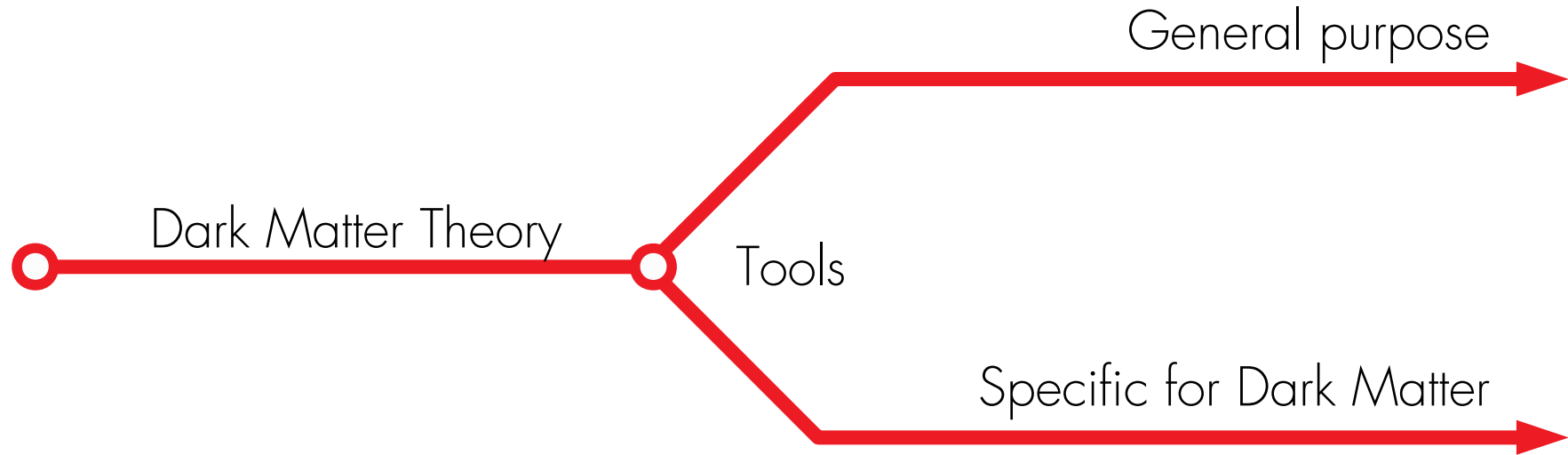


# Motivation

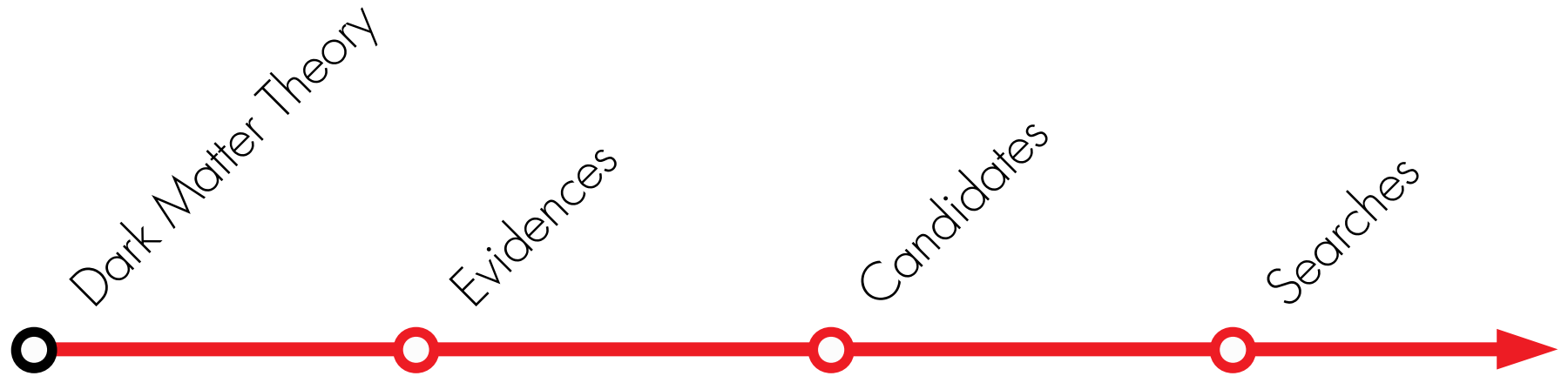
... but most of the tools are made by physicists to solve their own problems



# Course plan



# Today's plan





# Dark Matter: Evidences

# A little of history



1933: Fritz Zwicky postulated dark matter in order to explain Coma cluster dynamics as a bound system



<http://youtu.be/C8ZOgKlscEA>



# A little of history

## THE ASTROPHYSICAL JOURNAL

AN INTERNATIONAL REVIEW OF SPECTROSCOPY AND  
ASTRONOMICAL PHYSICS

VOLUME 86

OCTOBER 1937

NUMBER 3

### ON THE MASSES OF NEBULAE AND OF CLUSTERS OF NEBULAE

F. ZWICKY

#### ABSTRACT

Present estimates of the masses of nebulae are based on observations of the *luminosities* and *internal rotations* of nebulae. It is shown that both these methods are unreliable; that from the observed luminosities of extragalactic systems only lower limits for the values of their masses can be obtained (sec. i), and that from internal rotations alone no determination of the masses of nebulae is possible (sec. ii). The observed internal motions of nebulae can be understood on the basis of a simple mechanical model, some properties of which are discussed. The essential feature is a central core whose internal *viscosity* due to the gravitational interactions of its component masses is so high as to cause it to rotate like a solid body.

In sections iii, iv, and v three new methods for the determination of nebular masses are discussed, each of which makes use of a different fundamental principle of physics.

Method iii is based on the *virial theorem* of classical mechanics. The application of this theorem to the Coma cluster leads to a minimum value  $\bar{M} = 4.5 \times 10^{10} M_{\odot}$  for the average mass of its member nebulae.

Method iv calls for the observation among nebulae of certain *gravitational lens* effects.

Section v gives a generalization of the principles of ordinary *statistical mechanics* to the whole system of nebulae, which suggests a new and powerful method which ultimately should enable us to determine the masses of all types of nebulae. This method is very flexible and is capable of many modes of application. It is proposed, in particular, to investigate the distribution of nebulae in individual great clusters.

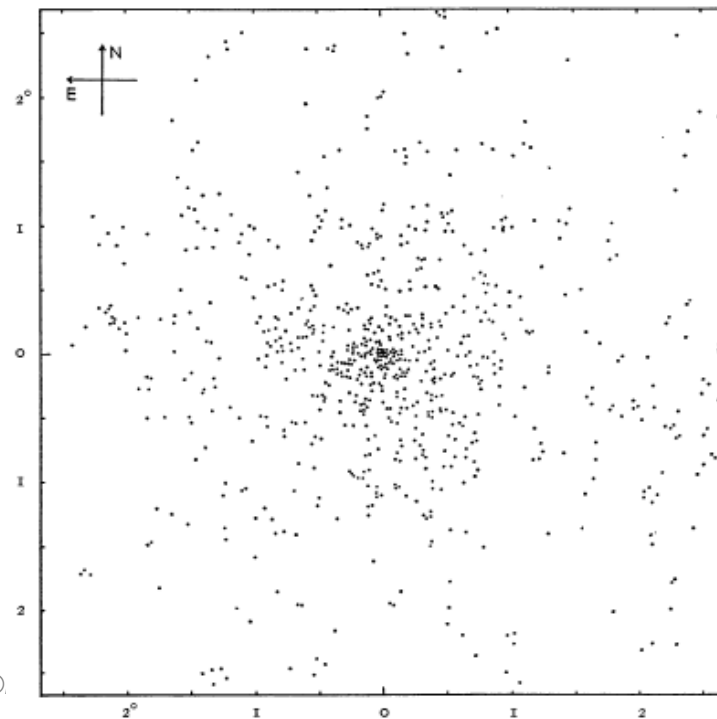
As a first step toward the realization of the proposed program, the Coma cluster of

THE MASSES OF NEBULAE

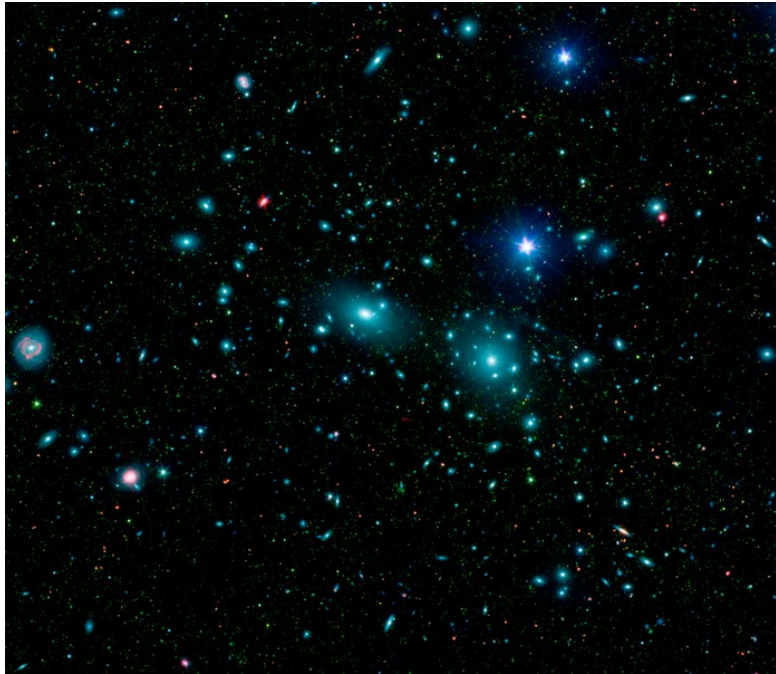
227

#### III. THE VIRIAL THEOREM APPLIED TO CLUSTERS OF NEBULAE

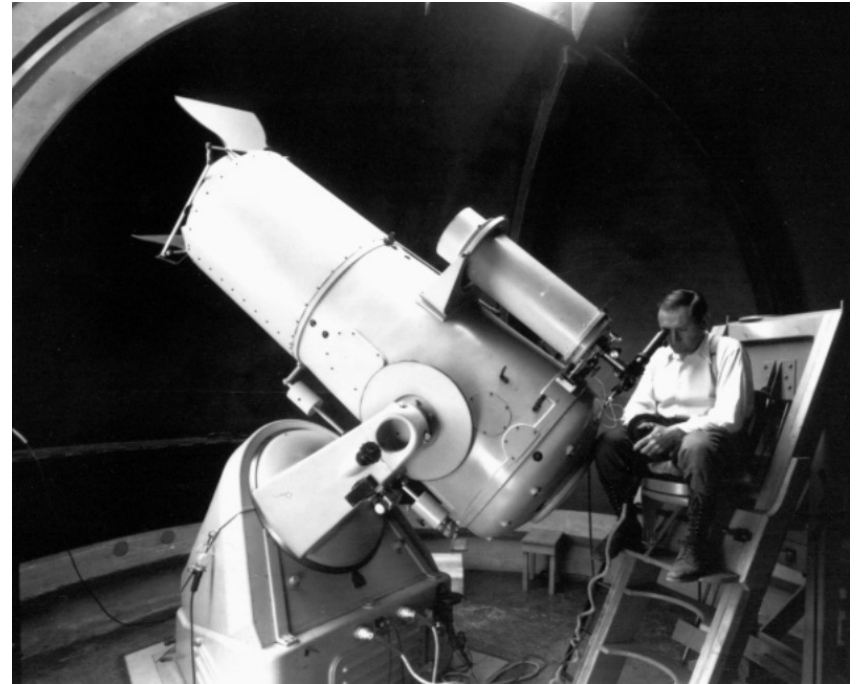
If the total masses of clusters of nebulae were known, the average masses of cluster nebulae could immediately be determined from counts of nebulae in these clusters, provided internebular material is of the same density inside and outside of clusters.



# A little of history



Coma Galaxy Cluster



Fritz Zwicky

Virial Theorem



**Dark Matter**



# Virial theorem

It relates global quantities of a system in equilibrium

$$\langle T \rangle = -\frac{1}{2} \sum_{k=1}^N \langle \vec{F}_k \cdot \vec{r}_k \rangle$$

For gravitationally bounded objects:

$$\langle T \rangle = -\frac{1}{2} \langle V_{\text{total}} \rangle \longrightarrow M_{\text{total}} \simeq \frac{2R_{\text{total}}\bar{v}^2}{G}$$

# A little of history



60's – 70's Vera Rubin studied rotation curves of many galaxies



Andromeda galaxy

# Doppler effect and redshift

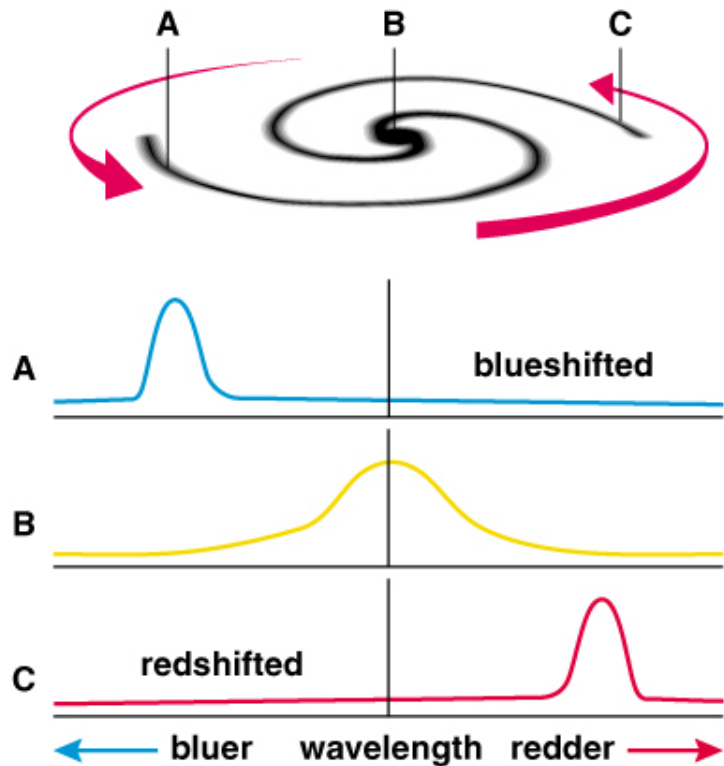
Observed redshift  $\longrightarrow z = \frac{\lambda_{\text{obs}} - \lambda_{\text{emit}}}{\lambda_{\text{emit}}}$

$1 + z = \frac{1 + v \cos \theta / c}{\sqrt{1 + v^2 / c^2}}$   $\longrightarrow$  Estimation of the velocity

$z > 0$  object going away

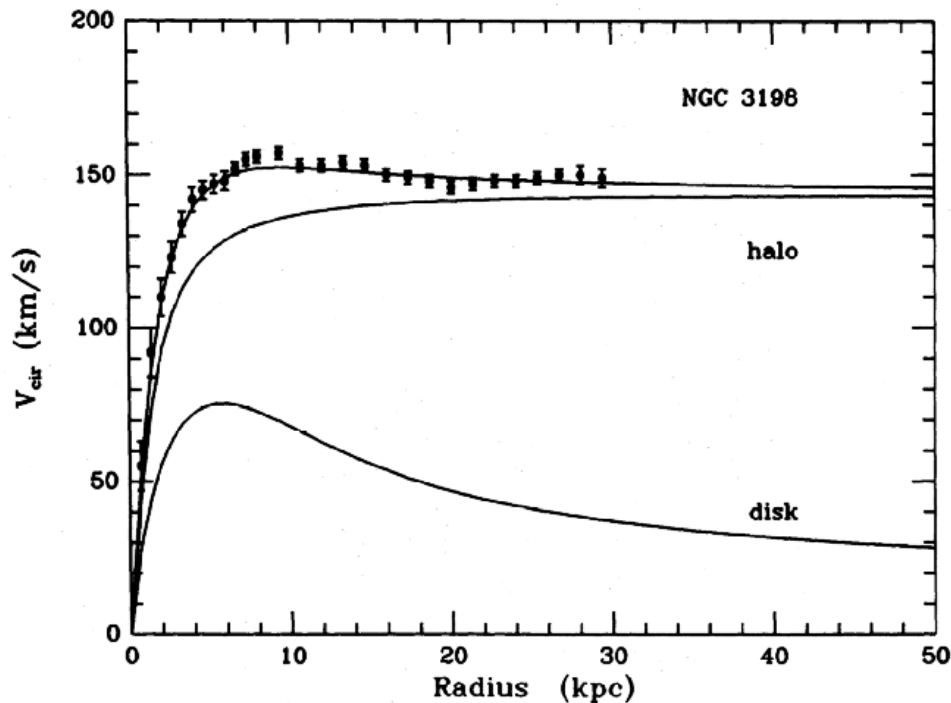
$z < 0$  object getting closer

# A little of history



Copyright © Addison Wesley.

60's – 70's **Vera Rubin** studied rotation curves of many galaxies

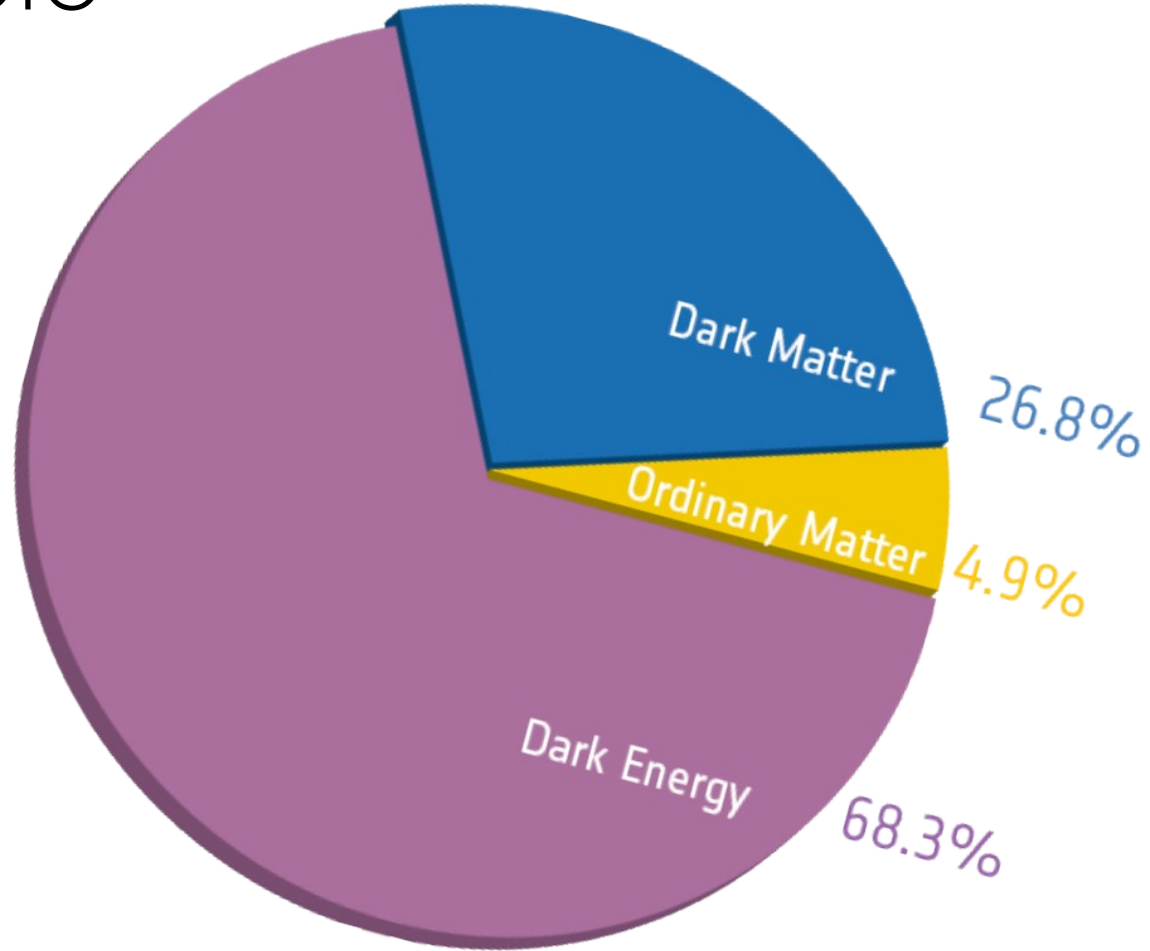




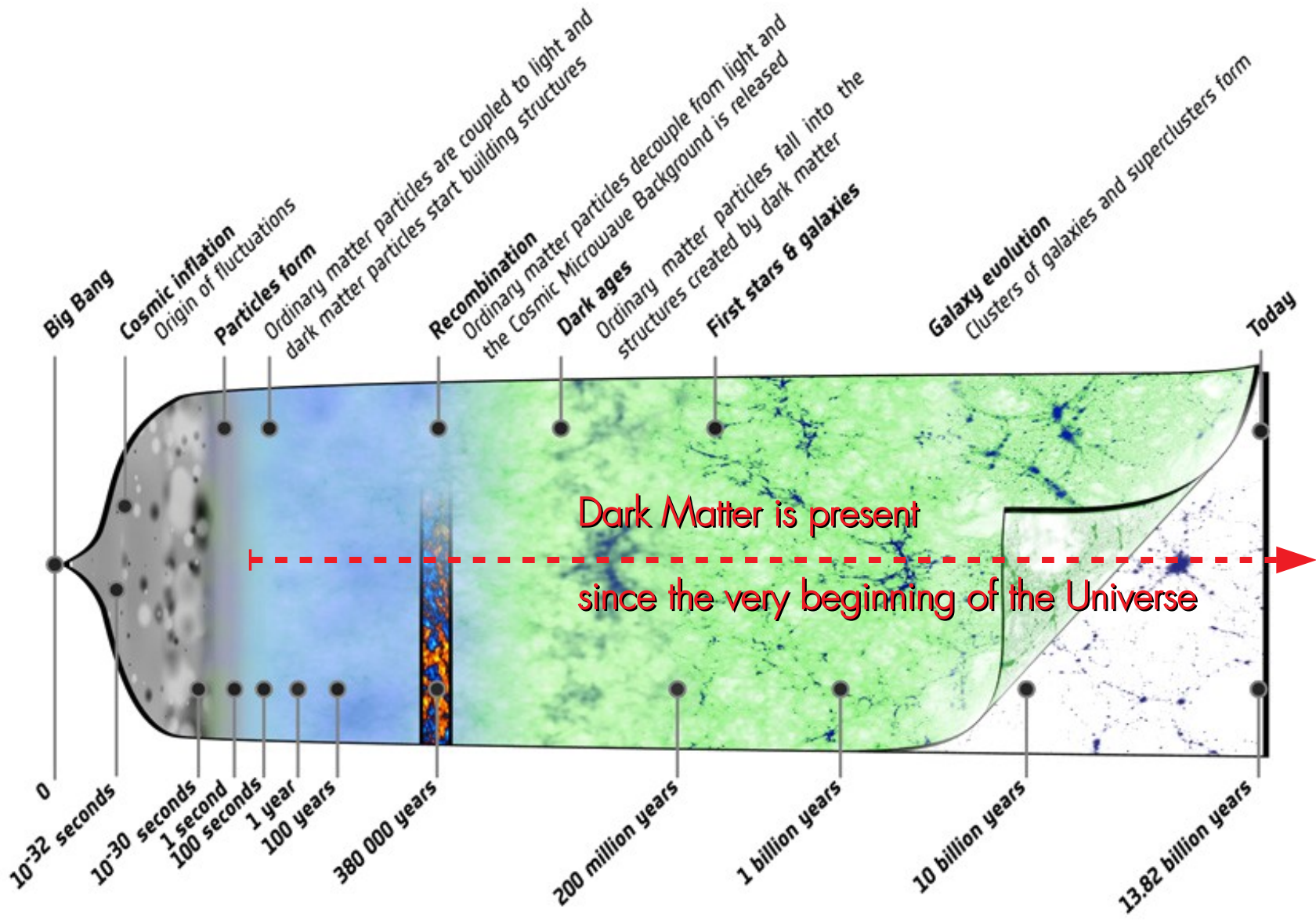
(short story)

Dark Matter is everywhere!

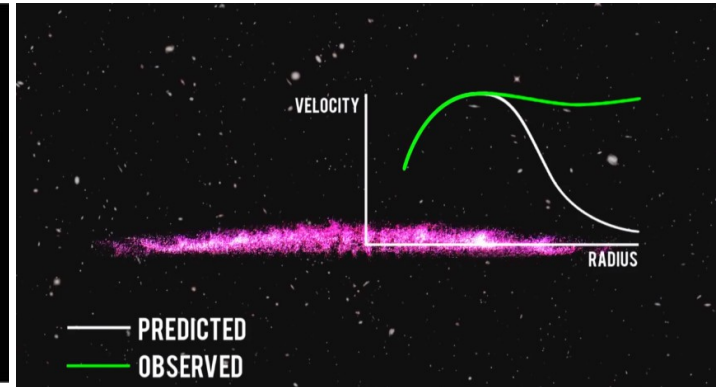
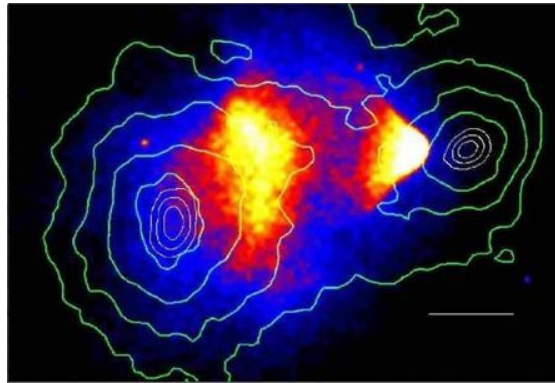
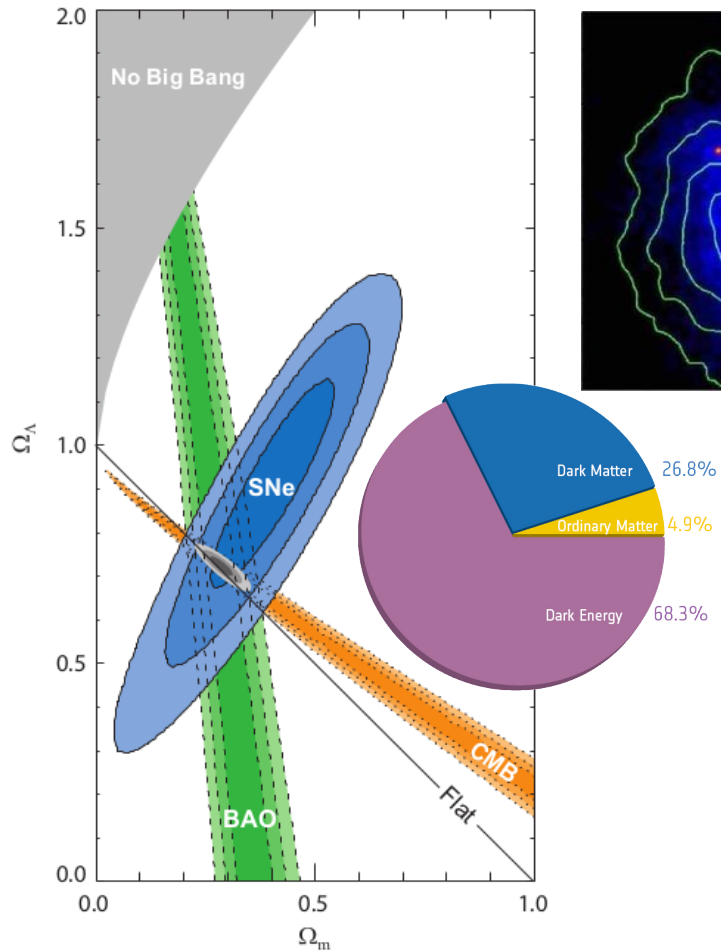
# Cosmic pie







# Dark Matter



Observations support Dark Matter

- Dynamics of clusters and galaxies
- Structure formation
- CMB anisotropies
- Baryon Acoustic Oscillation

$$\Omega_{\text{DM}} h^2 = 0.1196 \pm 0.0031$$

# Galactic scales

- Rotation curve
- Weak lensing
- Velocity dispersion of satellite galaxies
- Velocity dispersion of dSphs

# Galaxy cluster scales

- Velocity dispersion of individual galaxies
- Strong and weak lensing
- Peculiar velocity flows
- X-ray emission

# Cosmological scales

- CMB anisotropies
- Growth of structure
- LSS distribution
- BAOs
- SZ effect

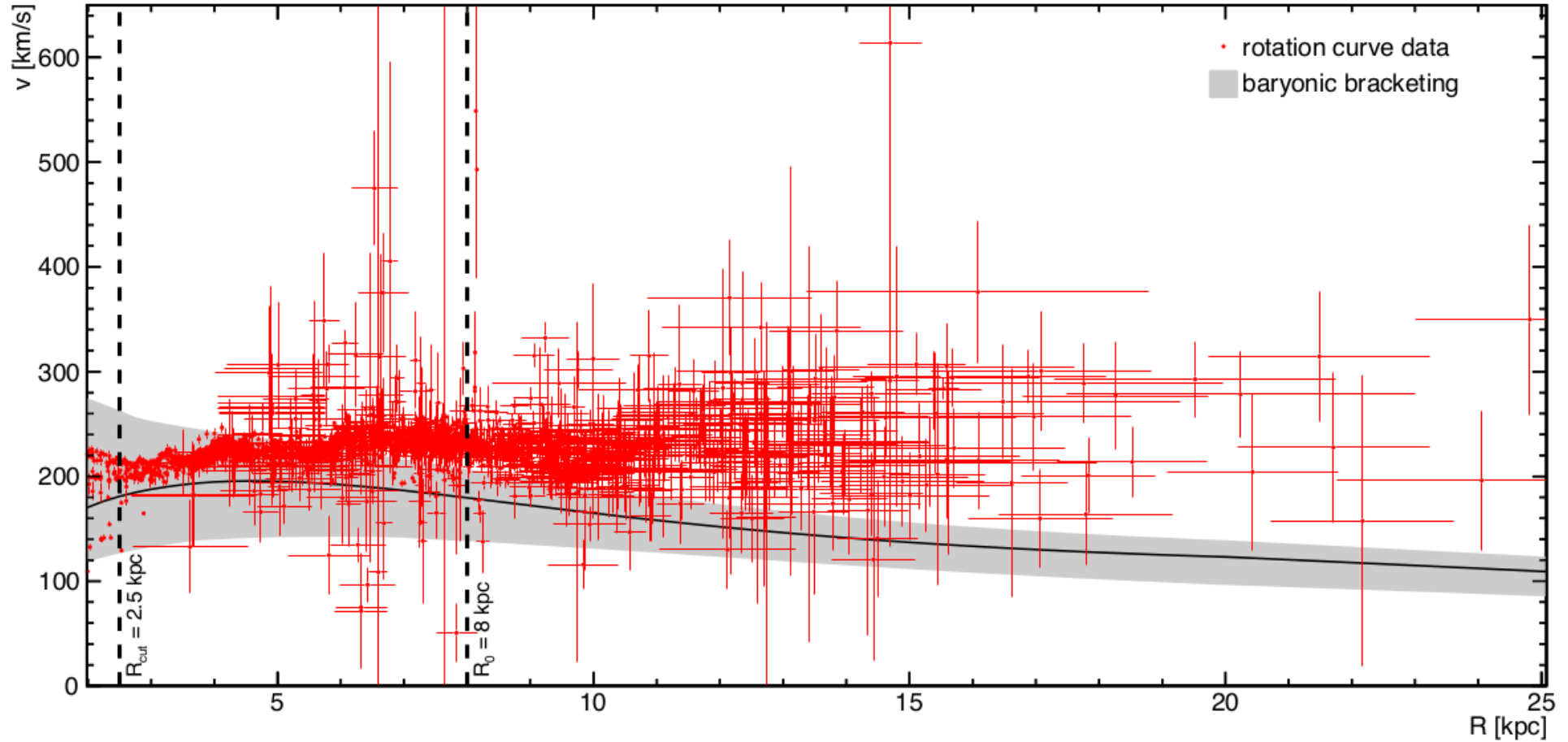


smaller  
kpc

larger  
Gpc

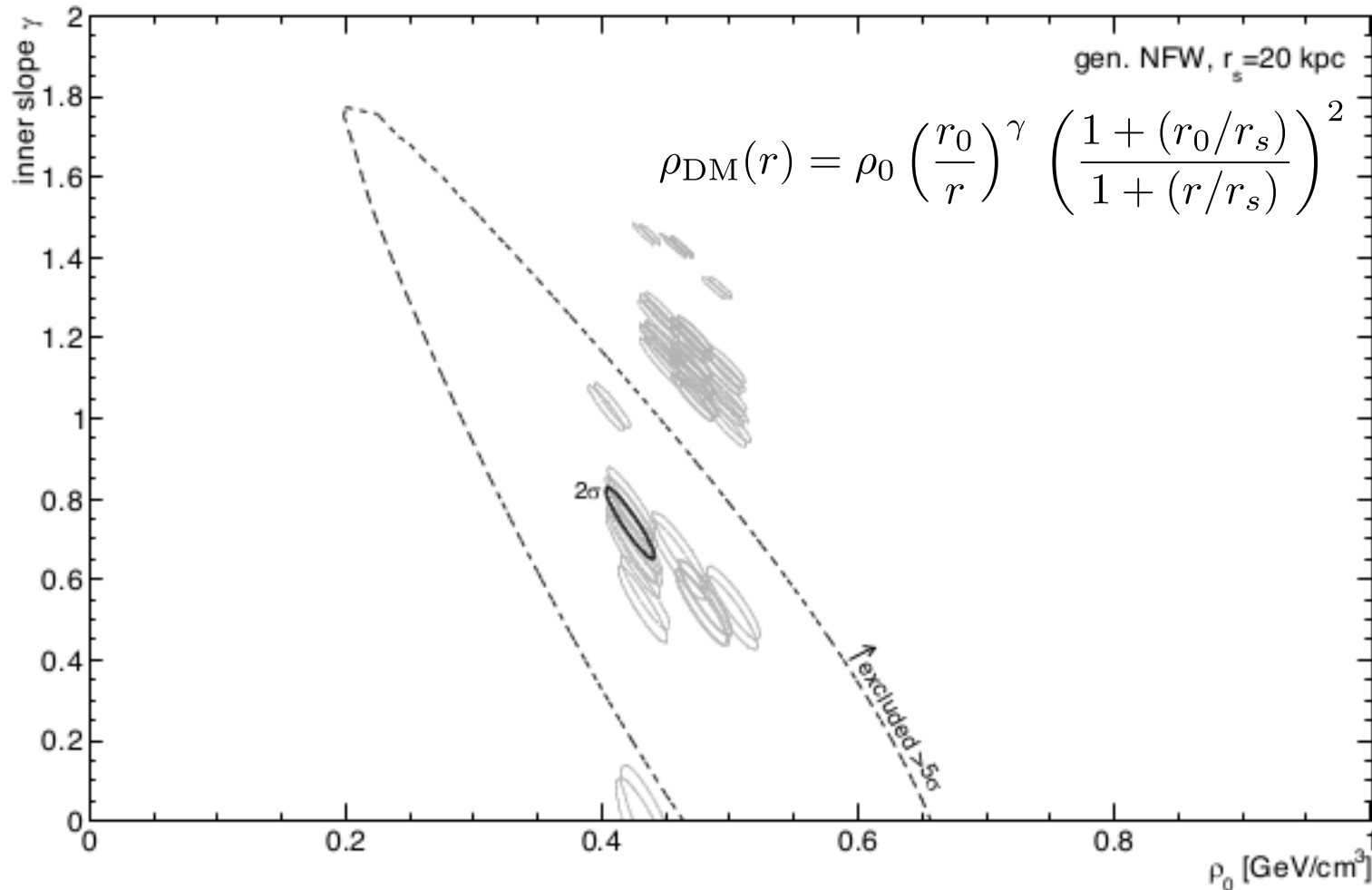
# Galactic scales

M. Pato et al JCAP 1512 (2015)



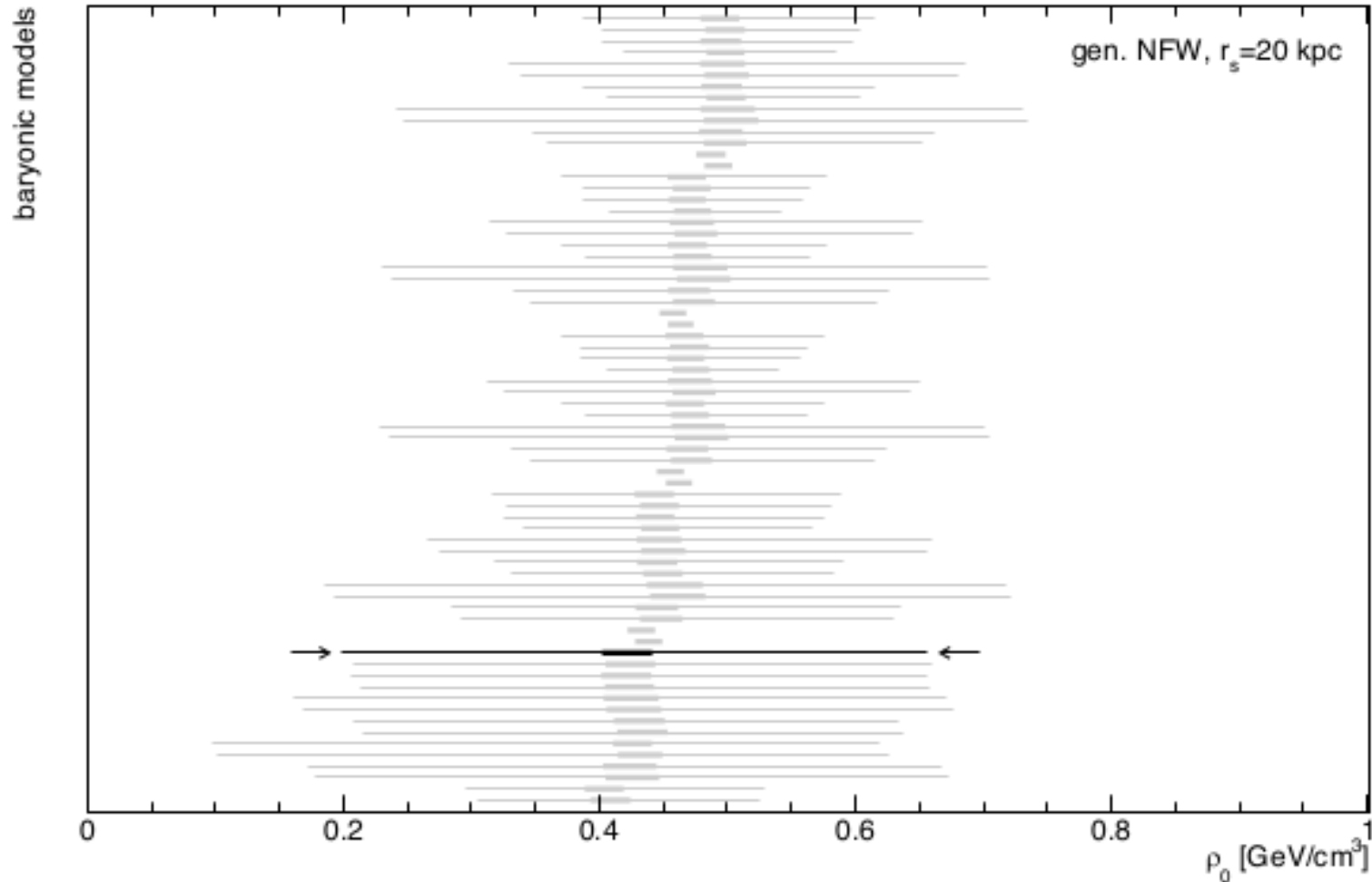
# Galactic scale

M. Pato et al JCAP 1512 (2015)



# Galactic scale

M. Pato et al JCAP 1512 (2015)



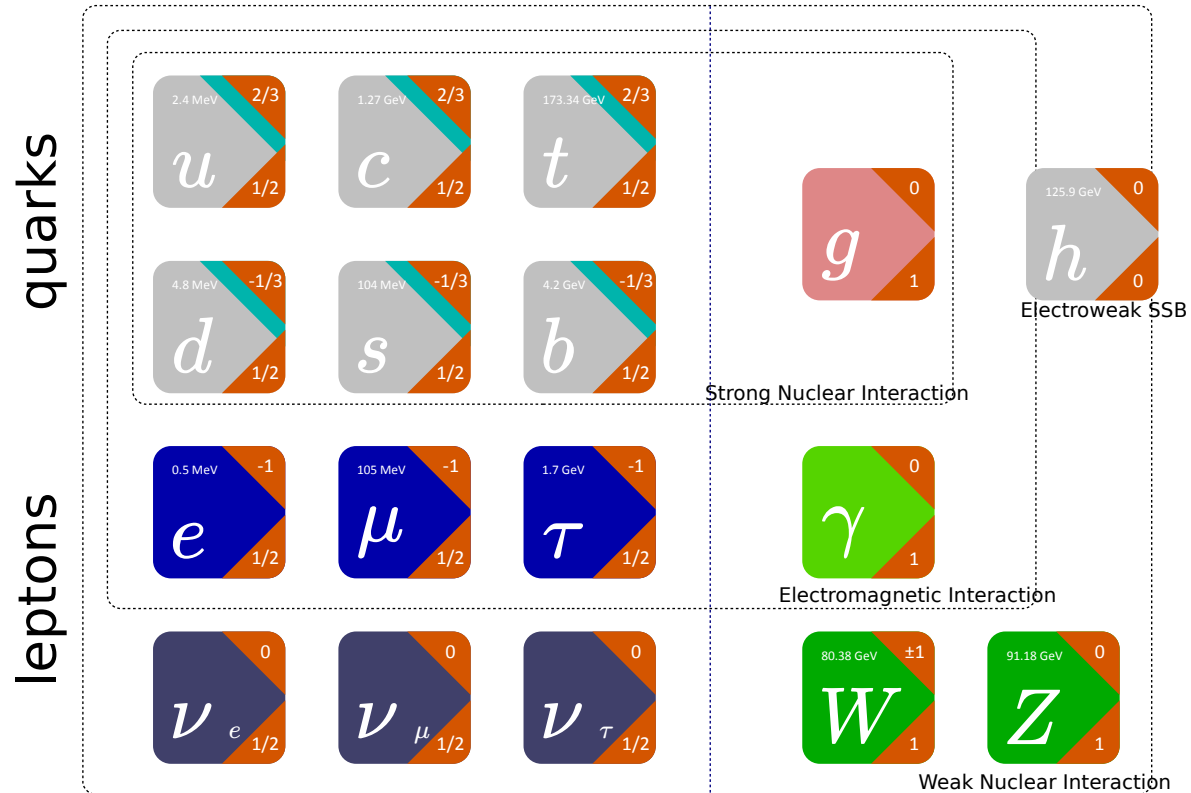
The background is a dense field of stars and galaxies. The stars are in various colors, including yellow, white, blue, and red. There are also several bright, multi-colored spots, likely representing distant galaxies or nebulae. The overall effect is a rich, multi-colored starfield.

# Dark Matter Candidates

(a small sample)

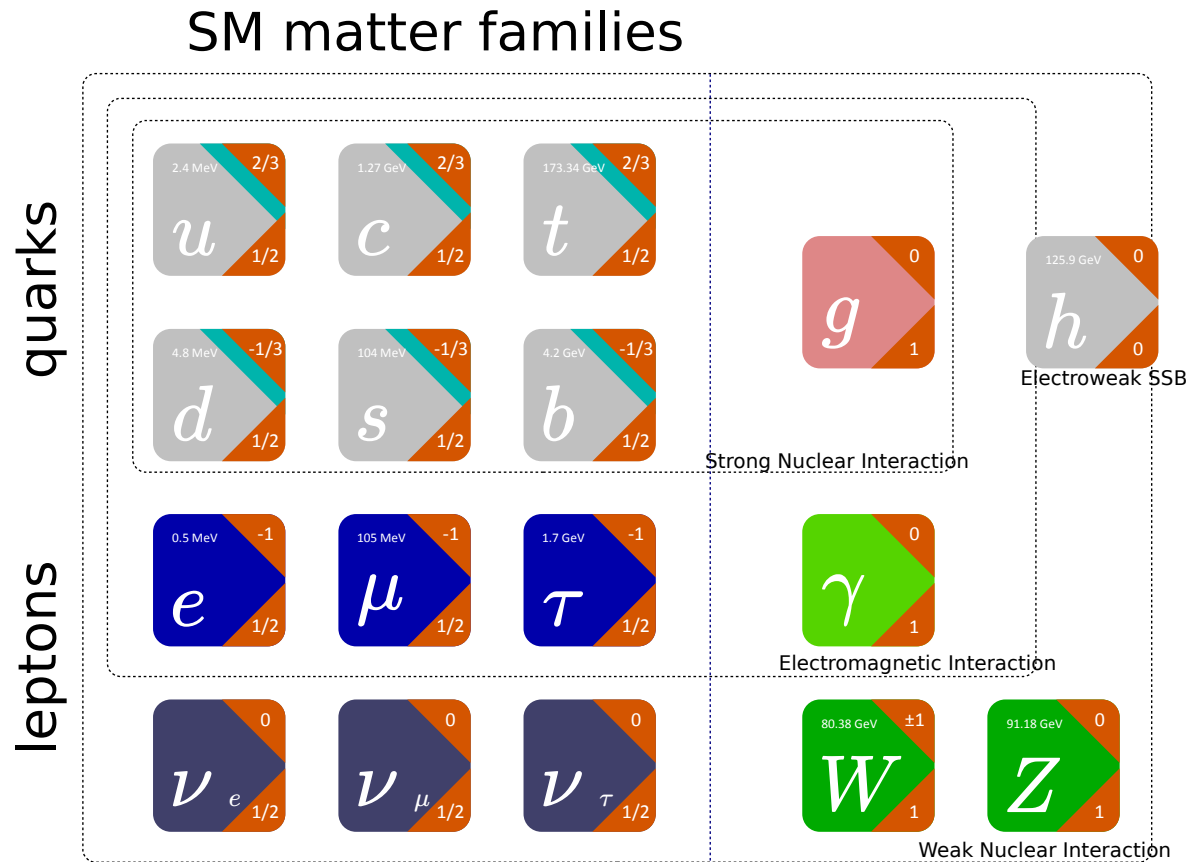
# The Standard Model (so far)

## SM matter families

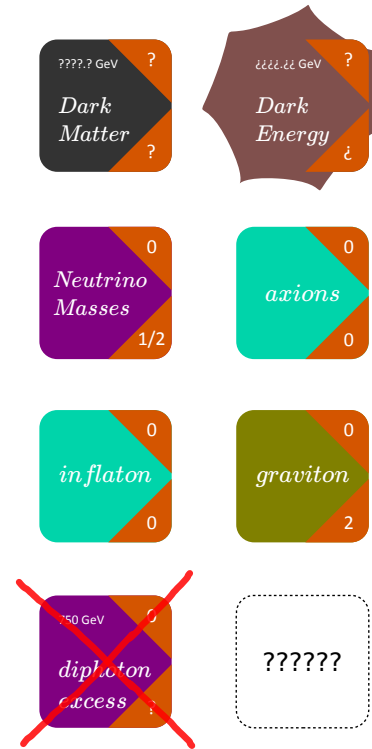




# The Standard Model (so far)



## Beyond SM



# Dark Matter particle properties

Massive

Non baryonic

Electrically neutral

Stable

# Dark Matter particle properties

Massive

Non baryonic

Electrically neutral

Stable



# Dark Matter particle properties

Massive (\*)

Non baryonic

Electrically neutral (\*\*)

Stable (\*\*\*)

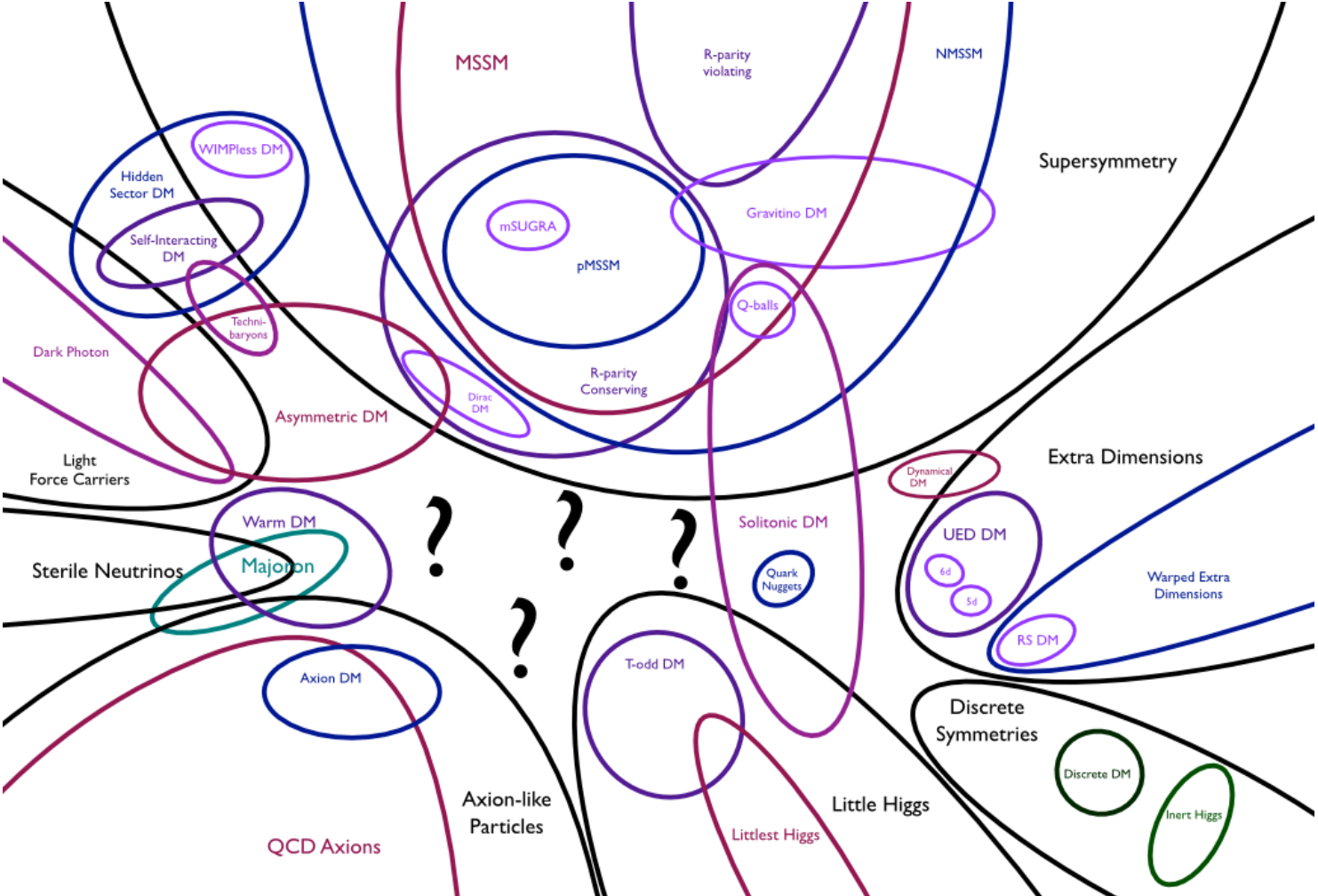
(\*) Its mass can go from  $10^{-22}$  eV to  $10^9$  GeV

(\*\*) Except **Milicharged DM** or **CHAMPs**

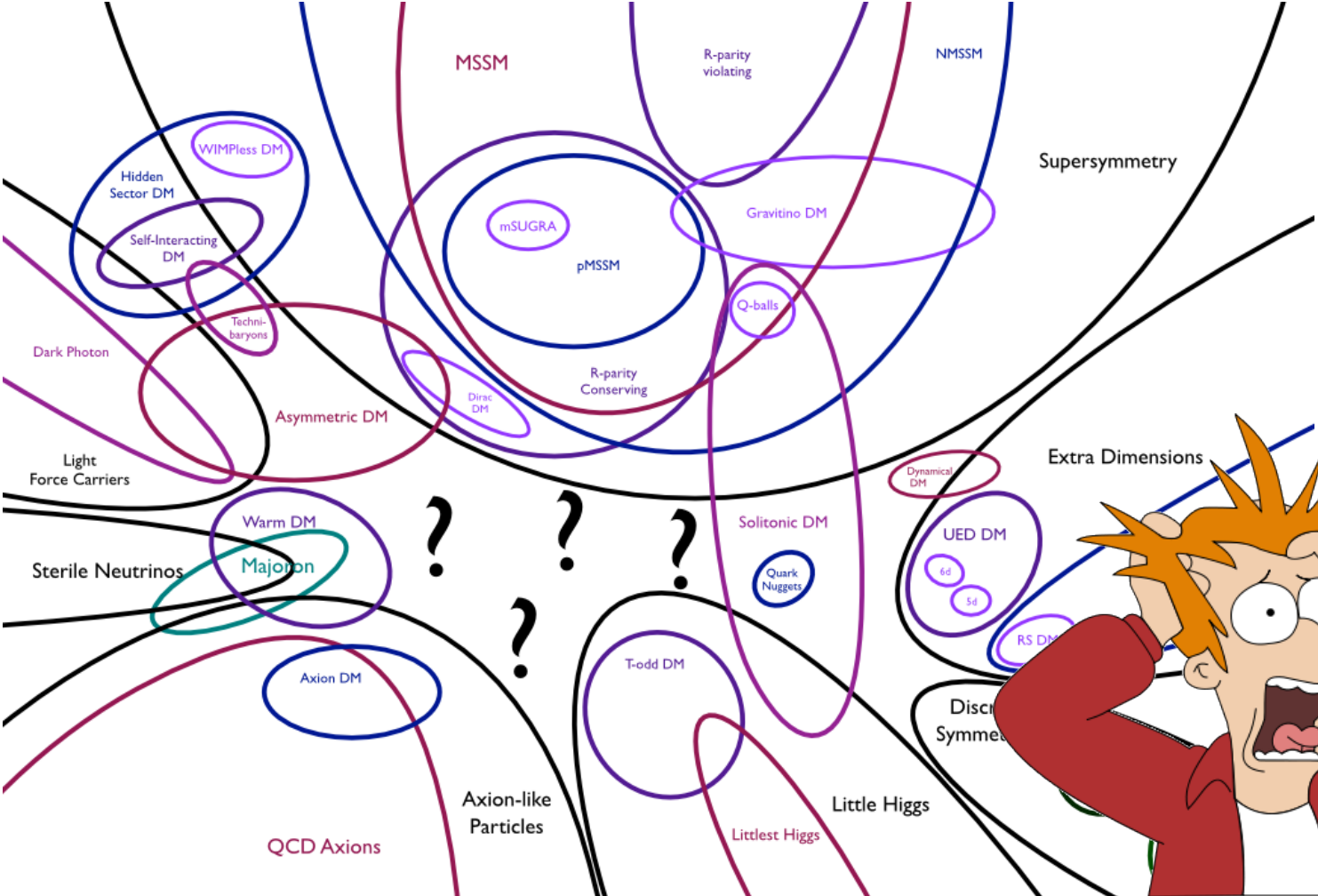
(\*\*\*) DM lifetime larger than  **$10^{27}$  seconds** (Universe =  $10^{17}$  seconds)



# Some candidates



# Some candidates





$\nu_s$


Sterile Neutrinos

# Sterile neutrinos

If right-handed neutrinos are part of the SM.  
They are natural SM gauge singlets

$$\mathcal{L}_2 = Y_2 \bar{L} H \nu_R$$

$$\mathcal{L}_R = \frac{1}{2} M_R \nu_R^T \nu_R + \text{h.c.}$$



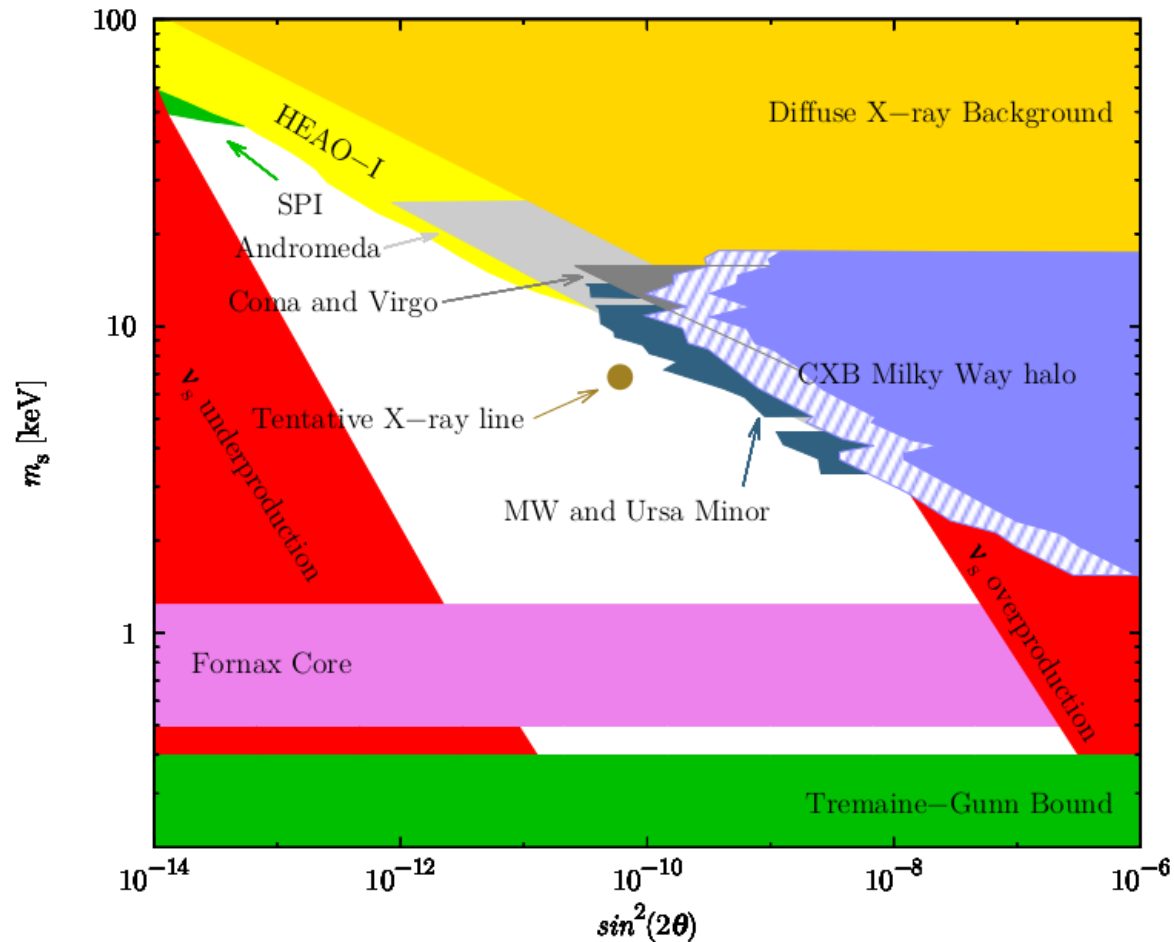
Two arrows point from the Lagrangian terms above to the mass matrix below. One arrow points from  $\mathcal{L}_2$  to the top-left element of the matrix, and the other points from  $\mathcal{L}_R$  to the bottom-right element.

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D \\ m_D & M_R \end{pmatrix}$$

Neutrino masses can be generated via the seesaw mechanism



# Sterile neutrinos



The background is a dense field of stars and galaxies in various colors, including yellow, orange, blue, and purple. A prominent pink and purple glow is centered behind the text.

ALPs

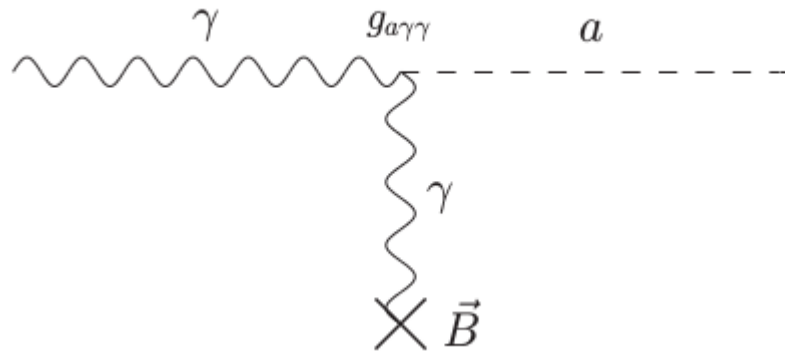
Axion like particles

# Axion Like Particles

Pseudo-Goldstone bosons.

$$\mathcal{L} = -\frac{1}{4}g_{\phi}\phi F_{\mu\nu}\tilde{F}^{\mu\nu}$$

Its main feature is the coupling to photons



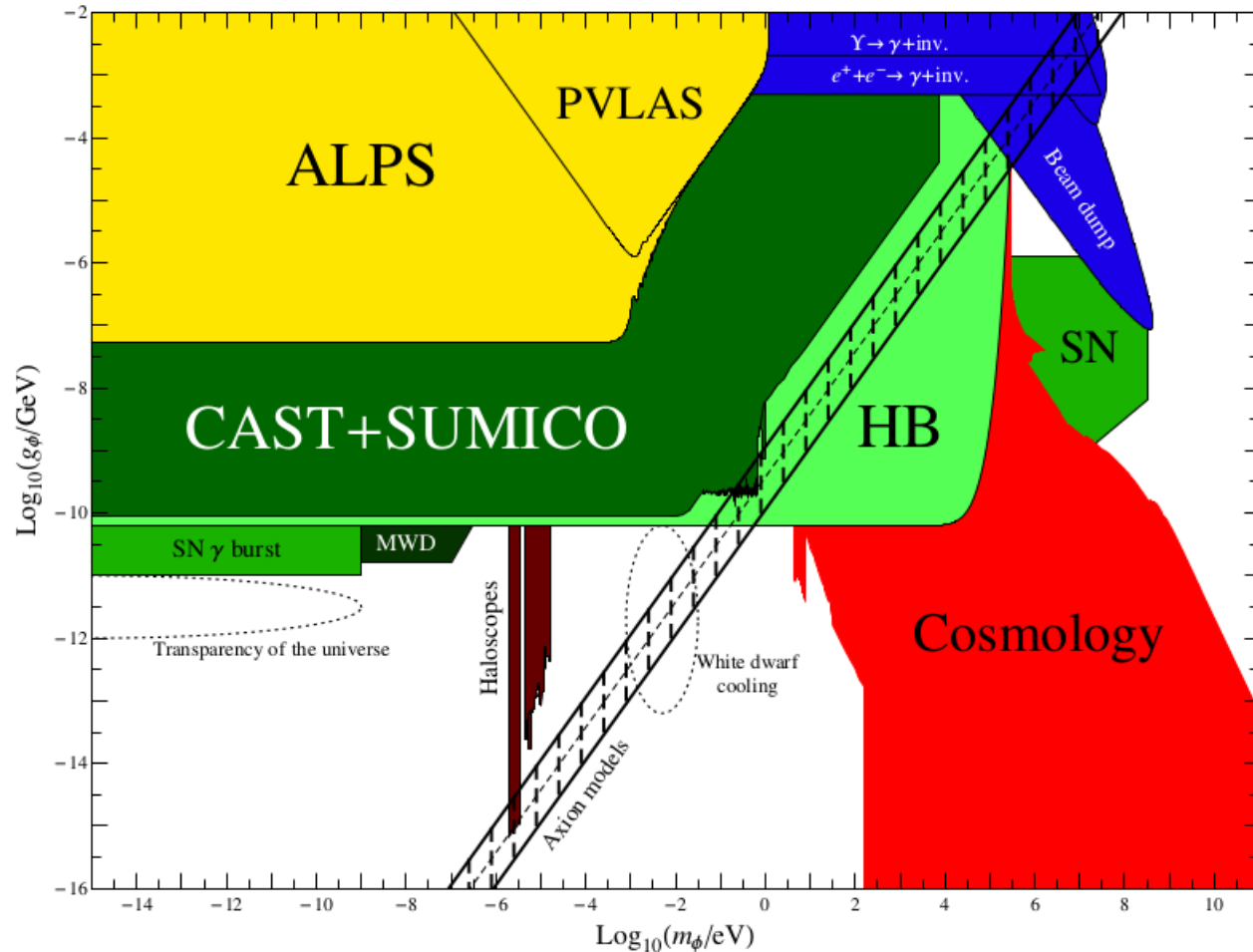
Primakoff effect

Searches involve photon emission line

Attenuation due to photon-axion conversion

See: [1210.3196](#)

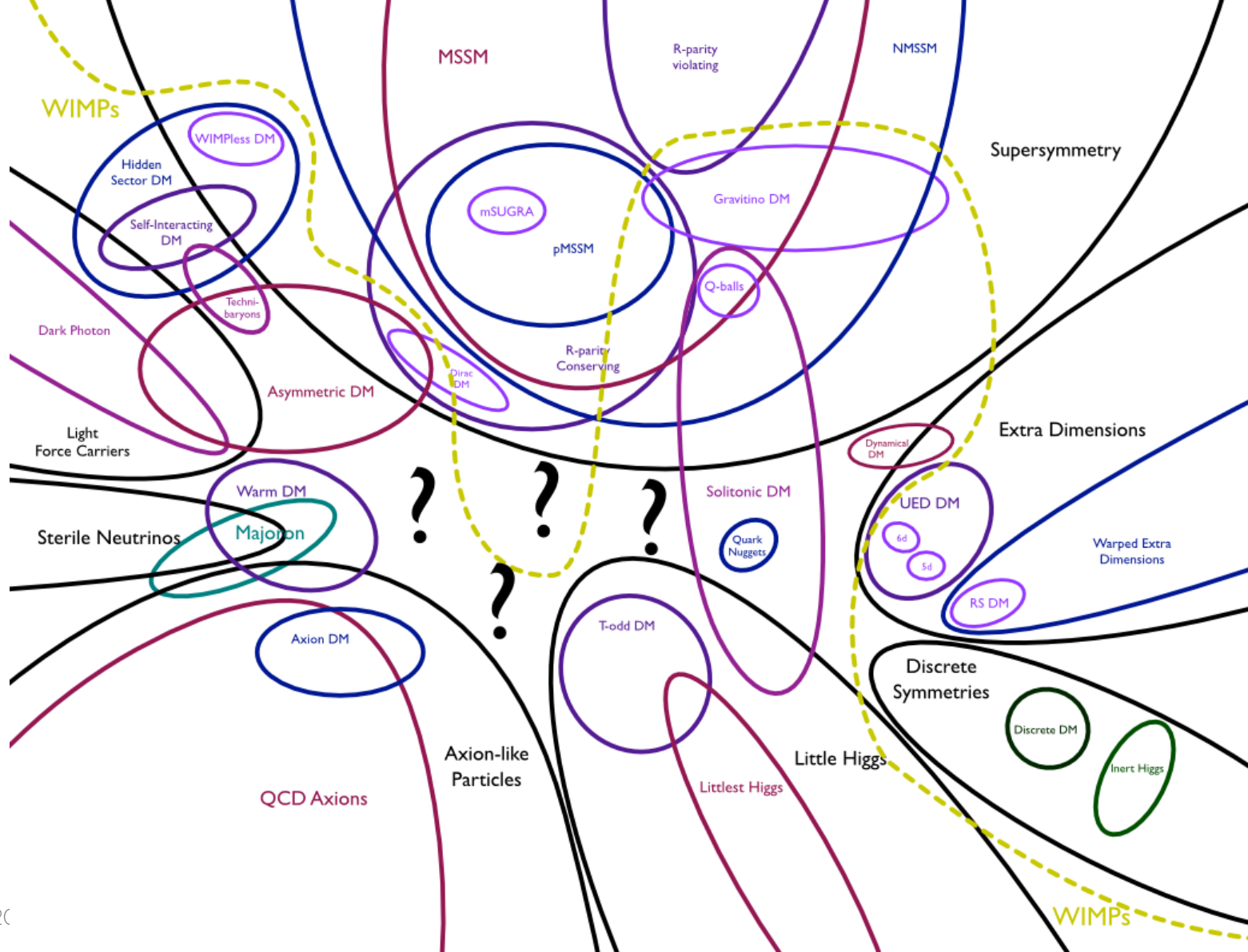
# Axion Like Particles



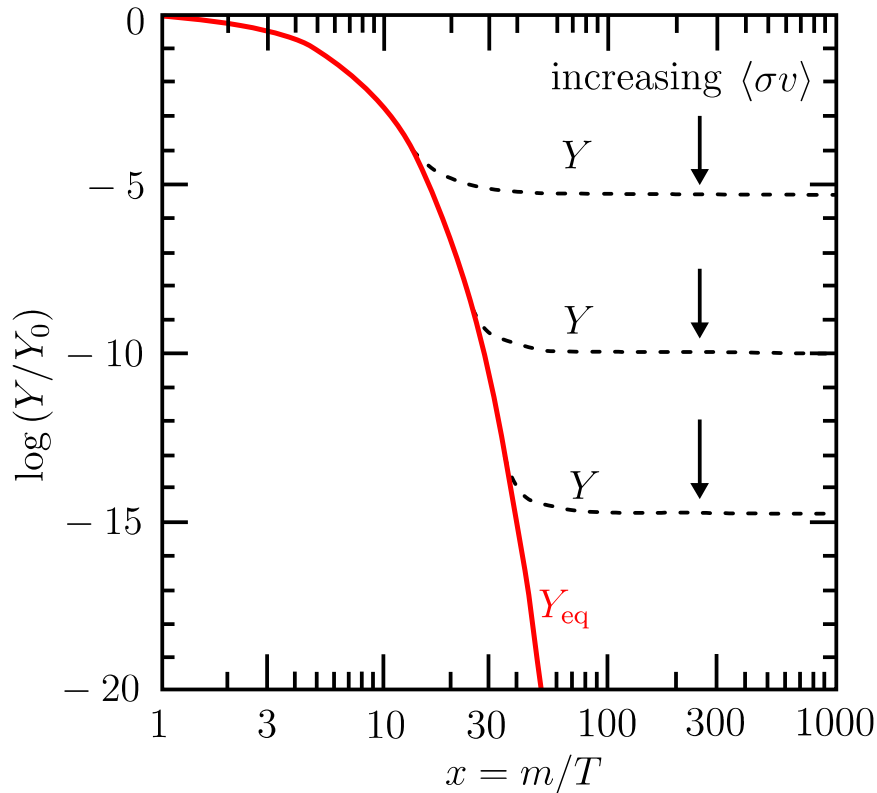


# WIMPs

Weakly Interactive Massive Particles



# WIMPs



Big Bang **Thermal** relic

Correct relic abundance for

$$\langle\sigma v\rangle \sim 1 \text{ pb} \cdot c$$

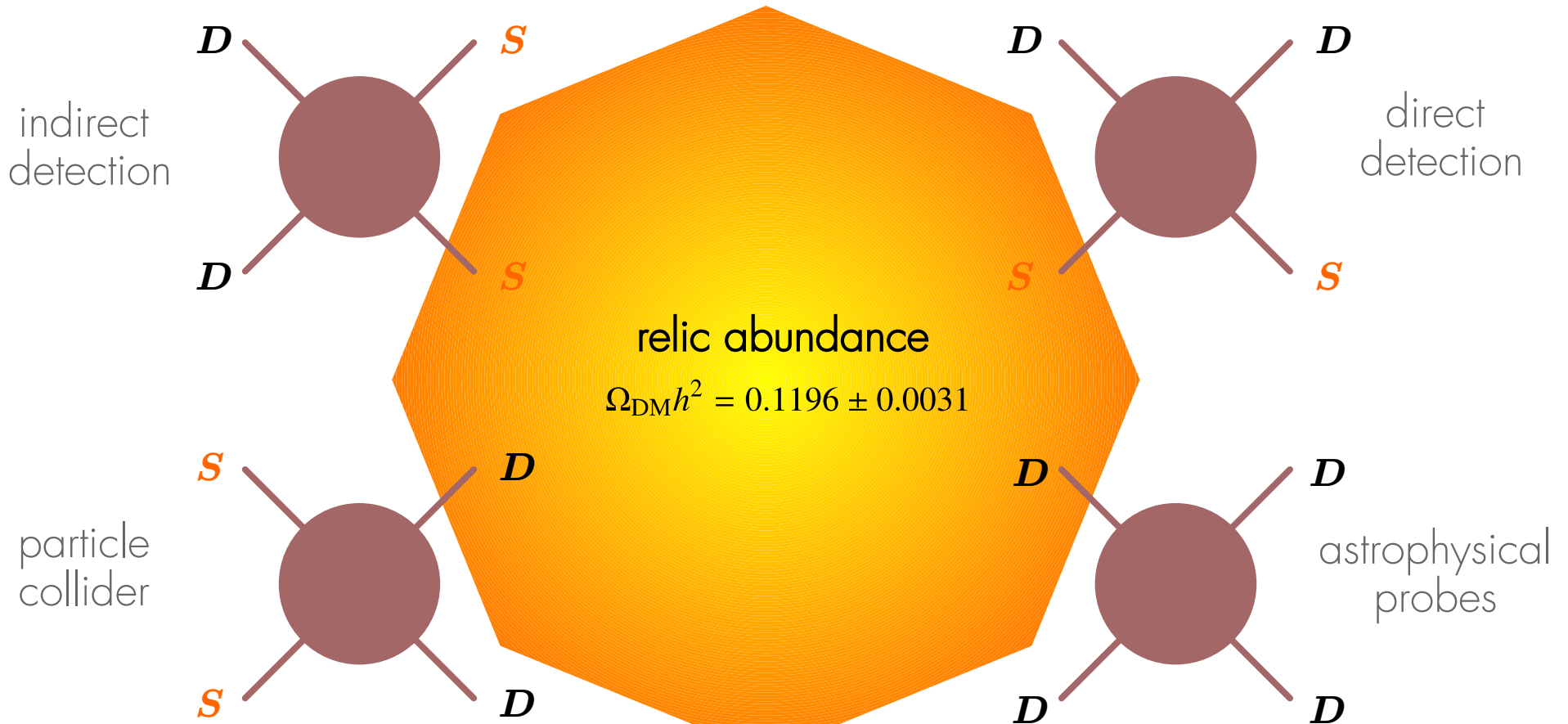
Mass in **GeV-TeV** range

For **WIMPs**:

$$\Omega_{\text{DM}} h^2 \simeq 0.1 \frac{3 \times 10^{-26} \text{ cm}^3/\text{s}}{\langle\sigma v\rangle_{\text{f.o.}}}$$

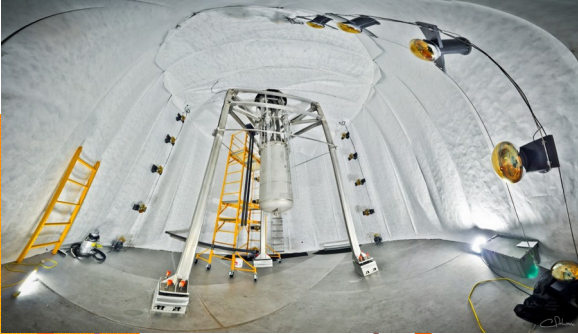
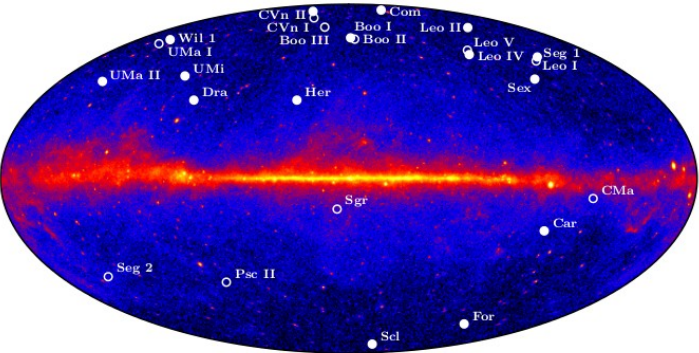
$$T_{\text{DM}}^{\text{f.o.}} \simeq \frac{1}{20} m_{\text{DM}}$$

# Dark Matter Searches





# Dark Matter Searches



relic abundance

$$\Omega_{\text{DM}} h^2 = 0.1196 \pm 0.0031$$



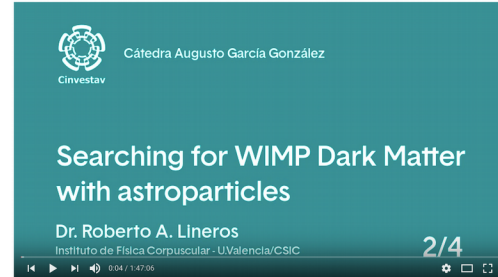


# Some extra details:



Búsqueda de Materia Oscura con astroparticulas 1/4

<https://youtu.be/DHc8Z2b1W5M>



Búsqueda de Materia Oscura con astroparticulas 2/4

<https://youtu.be/Gpi4vIQM348>



Búsqueda de Materia Oscura con astroparticulas 3/4

<https://youtu.be/Mxt33mN7sgU>



Búsqueda de Materia Oscura con astroparticulas 4/4

[https://youtu.be/y-dpl\\_FulQY](https://youtu.be/y-dpl_FulQY)



# Inert singlet DM model

The simplest DM model.

$$\mathcal{L} = \frac{1}{2} (\partial_\mu \phi)^2 - \frac{m_\phi}{2} \phi^2 - \frac{\lambda_\phi}{4} \phi^4 - \frac{\lambda_{\phi h}}{2} \phi^2 H^\dagger H + \mathcal{L}_{SM}$$

Features:

DM is a real scalar charged with a  $Z_2$  symmetry

The interaction with the SM is via Higgs particle

The relevant parameter are mass and coupling to the Higgs

# Inert singlet DM model

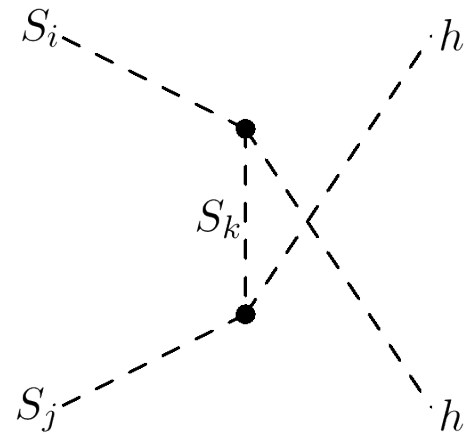
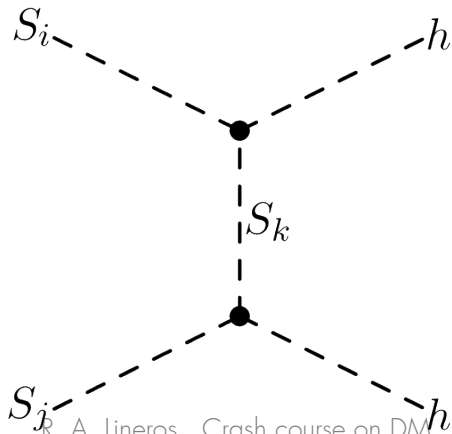
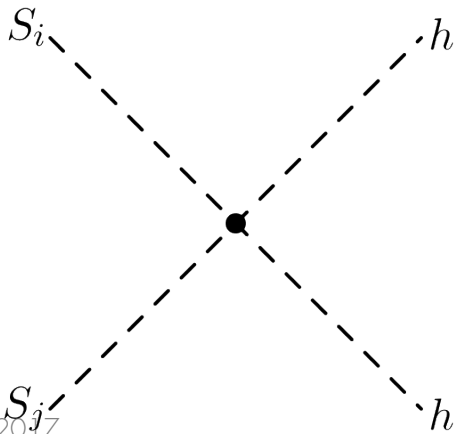
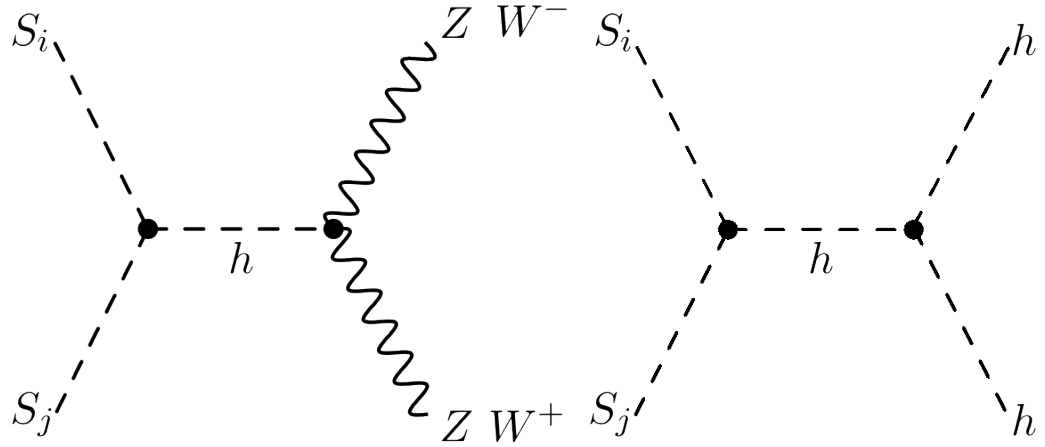
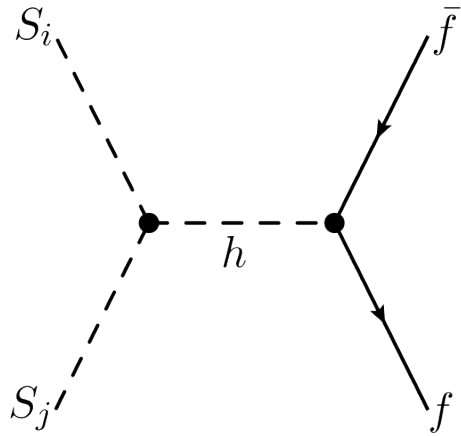
The simplest DM model.

$$\mathcal{L} = \frac{1}{2} (\partial_\mu \phi)^2 - \frac{m_\phi}{2} \phi^2 - \frac{\lambda_\phi}{4} \phi^4 - \frac{\lambda_{\phi h}}{2} \phi^2 H^\dagger H + \mathcal{L}_{SM}$$

Small exercise:

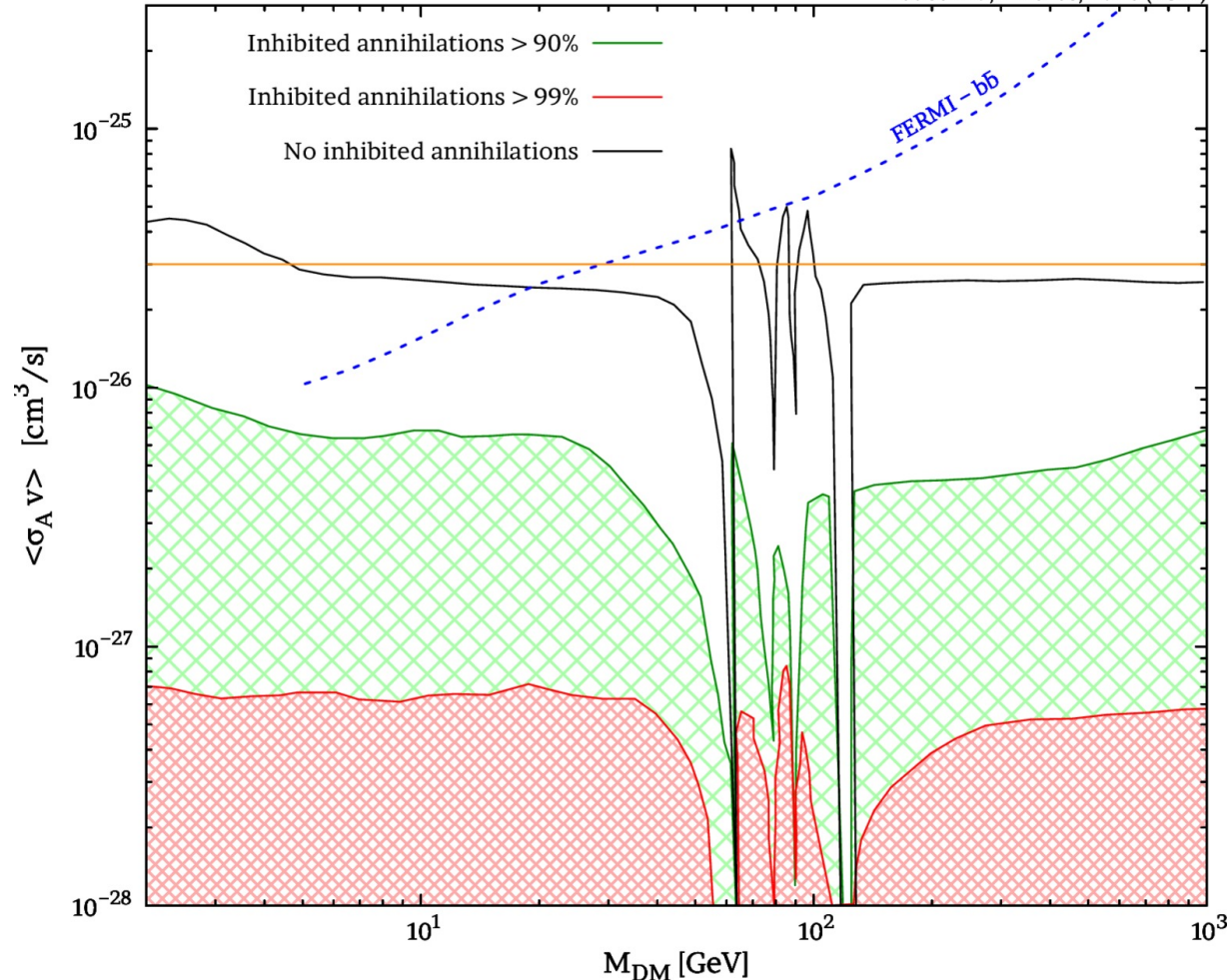
Draw diagrams relevant for the relic abundance

# Inert singlet DM model



# Inert singlet DM model

Boucenna, Lineros, Valle (2014)

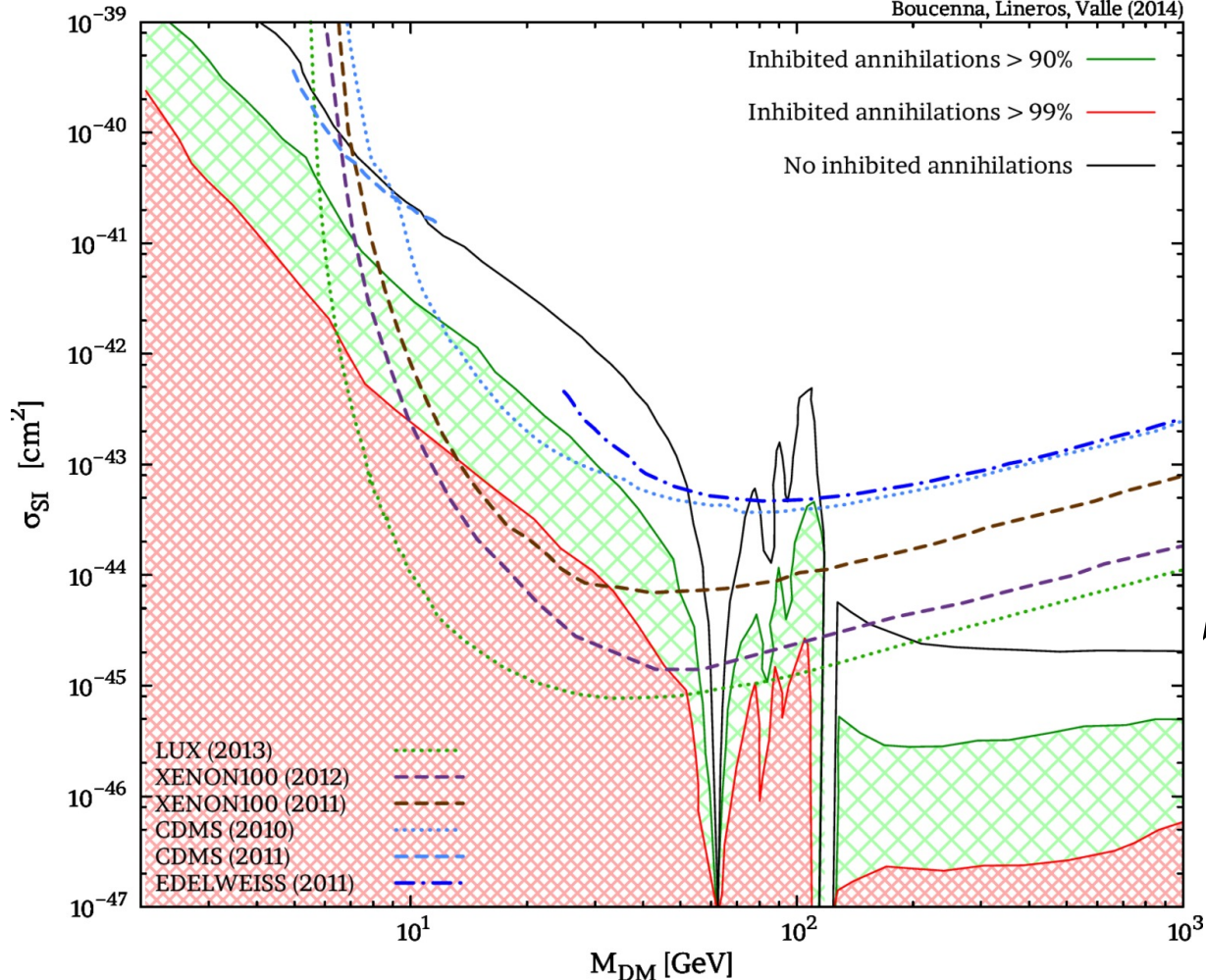


← Solution is the black line  
Tight relation among  
mass and higgs coupling



# Inert singlet DM model

Boucenna, Lineros, Valle (2014)



Solution is the black line

Tight relation among mass and higgs coupling

# Fermion singlet DM model

Dark Matter is a majorana fermion connected to the SM via a scalar singlet

$$\mathcal{L} = \frac{1}{2} \bar{\psi} (i\gamma_\mu \partial_\mu - m_\psi) \psi + \omega \phi \bar{\psi} \psi + \frac{1}{2} (\partial_\mu \phi)^2 - \frac{m_\phi^2}{2} \phi^2 - \frac{\lambda_1}{3} \phi^3 - \frac{\lambda_2}{4} \phi^4 - \frac{\lambda_3}{2} \phi H^\dagger H - \frac{\lambda_4}{2} \phi^2 H^\dagger H + \mathcal{L}_{SM}$$

The model contains:  
2 extra particles and 7  
parameters

More freedom to reproduce DM  
observables

Small exercise:

Draw diagrams  
relevant for the relic  
abundance

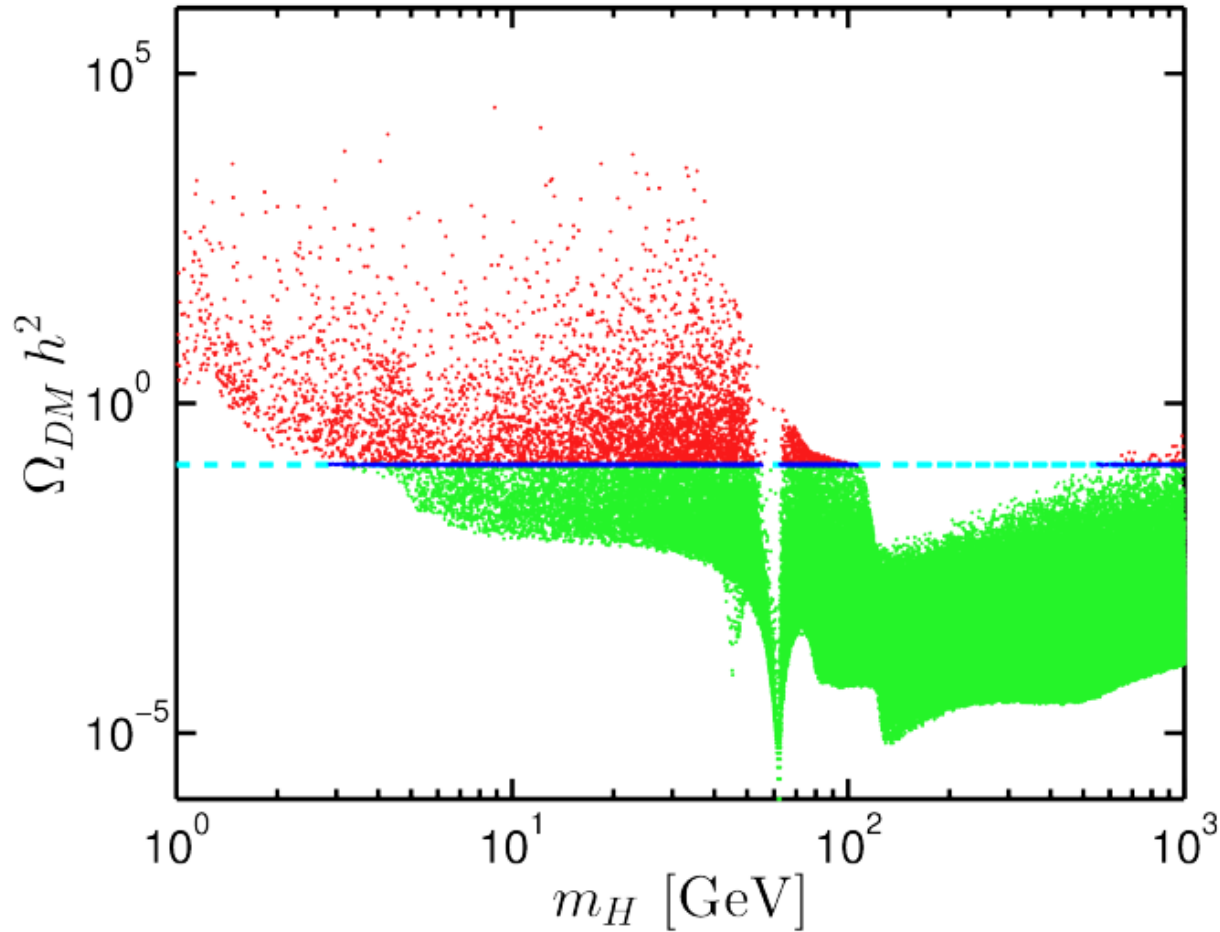
# Inert Higgs DM model

DM is part of a  $SU(2)$  scalar doublet (copy of Higgs) but charged with a  $Z_2$  symmetry

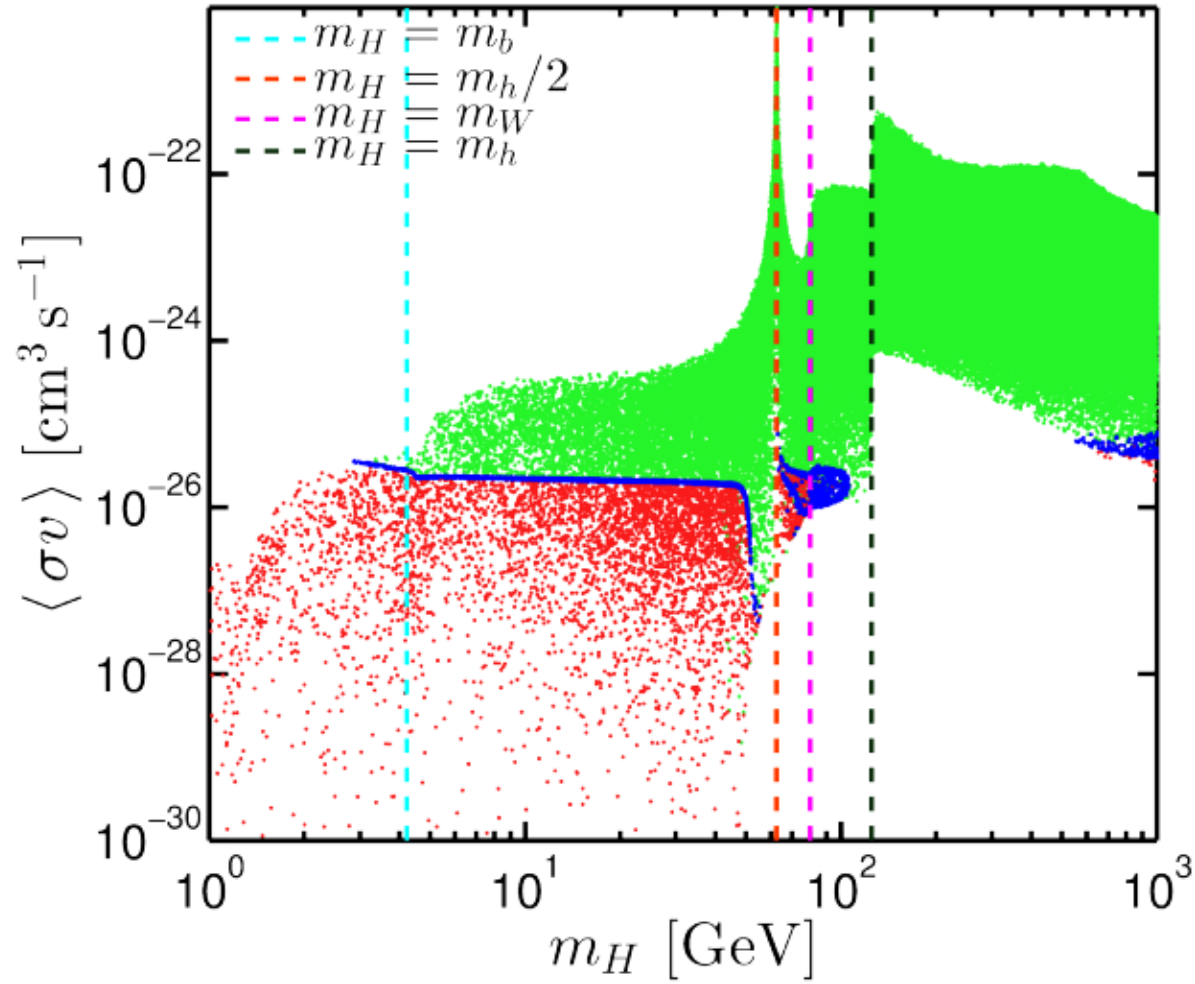
$$V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} \left[ (H_1^\dagger H_2)^2 + \text{h.c.} \right],$$

$$H_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h + iG^0) \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(S + iA) \end{pmatrix}$$

# Inert Higgs DM model



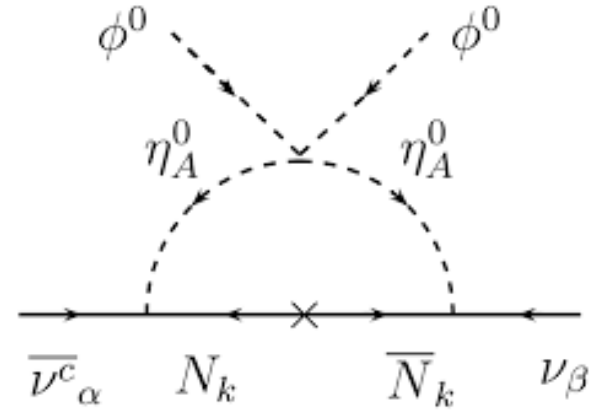
# Inert Higgs DM model



# Scotogenic DM model (Ma, 2006... and many other papers)

Model provides a mechanism where neutrino acquire mass via loop.

Inside the loop DM particles run.



$$(\mathcal{M}_\nu)_{ij} = \sum_k \frac{h_{ik} h_{jk} M_k}{16\pi^2} \left[ \frac{m_R^2}{m_R^2 - M_k^2} \ln \frac{m_R^2}{M_k^2} - \frac{m_I^2}{m_I^2 - M_k^2} \ln \frac{m_I^2}{M_k^2} \right],$$

# Scotogenic DM model

$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{2} M_i \overline{N}_i N_i^c + h_{ij} \overline{N}_i \tilde{\eta}^\dagger \ell^j + \text{h.c.}$$

$$\begin{aligned} V = & m_H^2 \phi^\dagger \phi + m_\eta^2 \eta^\dagger \eta + \frac{\lambda_1}{2} (\phi^\dagger \phi)^2 \\ & + \frac{\lambda_2}{2} (\eta^\dagger \eta)^2 + \lambda_3 (\phi^\dagger \phi) (\eta^\dagger \eta) \\ & + \lambda_4 (\phi^\dagger \eta) (\eta^\dagger \phi) + \left[ \frac{\lambda_5}{2} (\eta^\dagger \phi)^2 + \text{h.c.} \right] \end{aligned}$$

# Singlet-Triplet Scotogenic DM

DM is mix between a singlet fermion and a  $SU(2)$  triplet

	Standard Model			Fermions		Scalars	
	$L$	$e$	$\phi$	$\Sigma$	$N$	$\eta$	$\Omega$
$SU(2)_L$	2	1	2	3	1	2	3
$Y$	-1	-2	1	0	0	1	0
$Z_2$	+	+	+	-	-	-	+

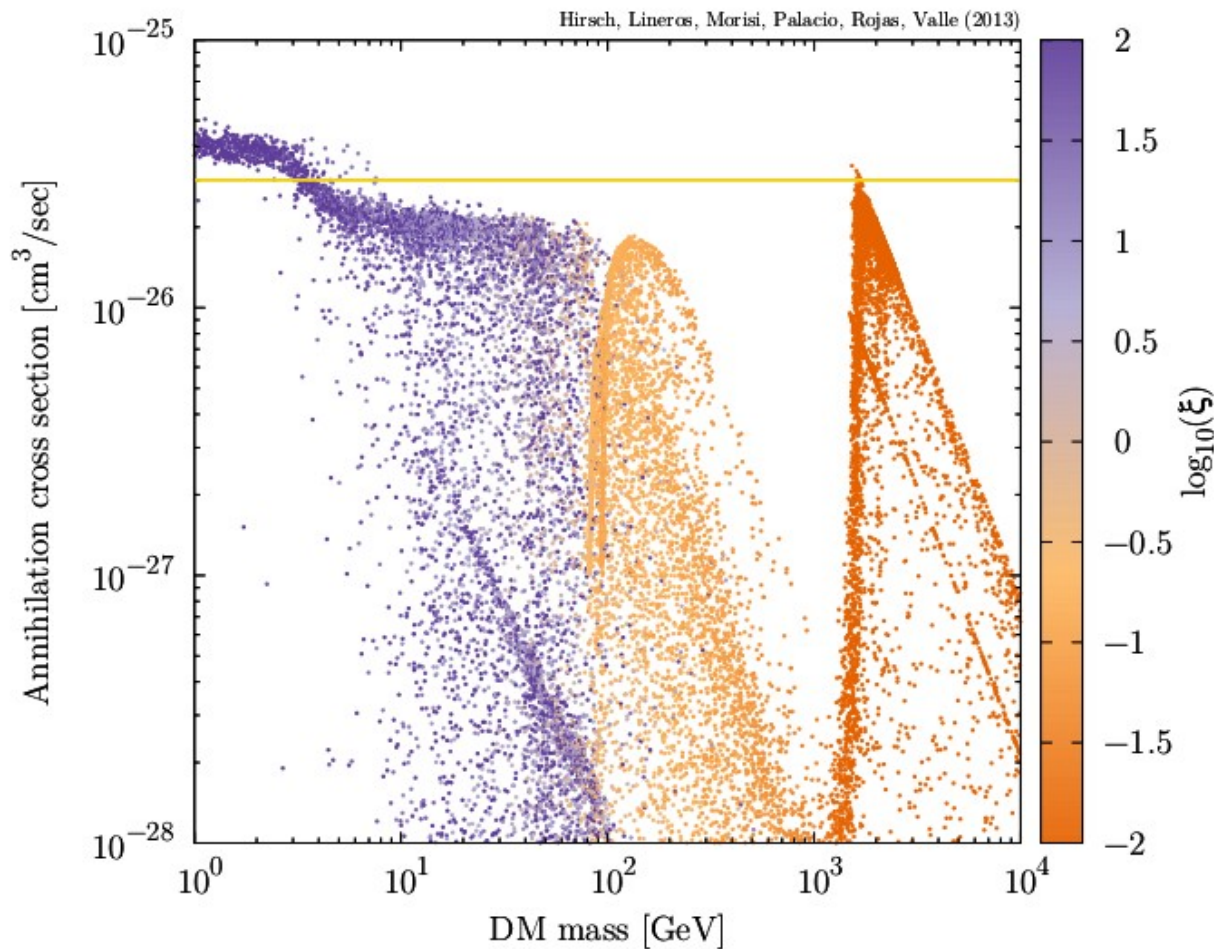


# Singlet-Triplet Scotogenic DM

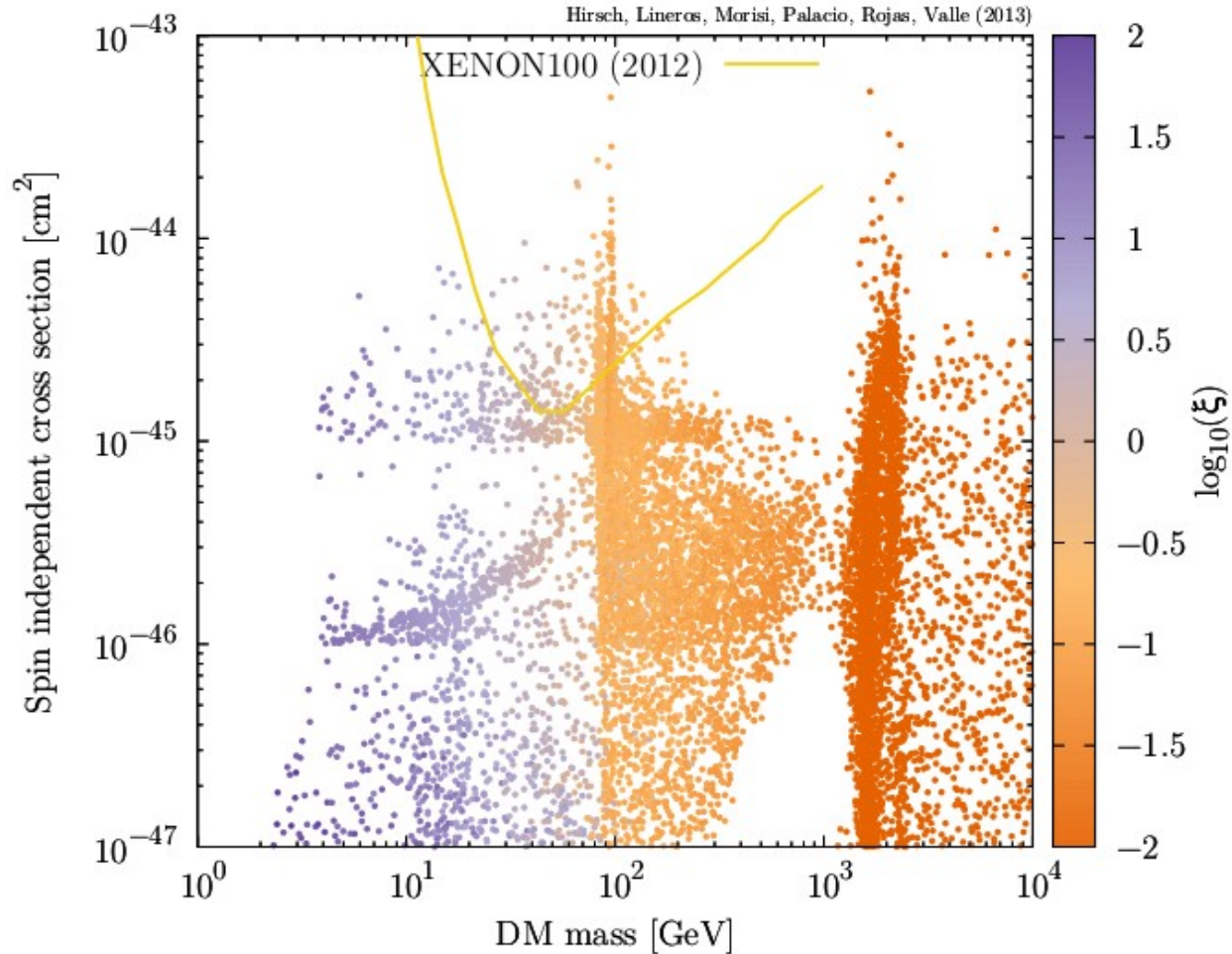
$$\mathcal{L} \supset -Y_{\alpha\beta} \bar{L}_\alpha e_\beta \phi - Y_{\Sigma_\alpha} \bar{L}_\alpha C \Sigma^\dagger \tilde{\eta} - \frac{1}{4} M_\Sigma \text{Tr} [\bar{\Sigma}^c \Sigma] + \\ -Y_\Omega \text{Tr} [\bar{\Sigma} \Omega] N - Y_{N_\alpha} \bar{L}_\alpha \tilde{\eta} N - \frac{1}{2} M_N \bar{N}^c N + h.c.$$

$$V_{\text{scal}} = -m_1^2 \phi^\dagger \phi + m_2^2 \eta^\dagger \eta + \frac{\lambda_1}{2} (\phi^\dagger \phi)^2 + \frac{\lambda_2}{2} (\eta^\dagger \eta)^2 + \lambda_3 (\phi^\dagger \phi) (\eta^\dagger \eta) \\ + \lambda_4 (\phi^\dagger \eta) (\eta^\dagger \phi) + \frac{\lambda_5}{2} (\phi^\dagger \eta)^2 + h.c. - \frac{M_\Omega^2}{4} \text{Tr} (\Omega^\dagger \Omega) + (\mu_1 \phi^\dagger \Omega \phi + h.c.) \\ + \lambda_1^\Omega \phi^\dagger \phi \text{Tr} (\Omega^\dagger \Omega) + \lambda_2^\Omega (\text{Tr}(\Omega^\dagger \Omega))^2 + \lambda_3^\Omega \text{Tr}((\Omega^\dagger \Omega)^2) + \lambda_4^\Omega (\phi^\dagger \Omega) (\Omega^\dagger \phi) \\ + (\mu_2 \eta^\dagger \Omega \eta + h.c.) + \lambda_1^\eta \eta^\dagger \eta \text{Tr} (\Omega^\dagger \Omega) + \lambda_4^\eta (\eta^\dagger \Omega) (\Omega^\dagger \eta) ,$$

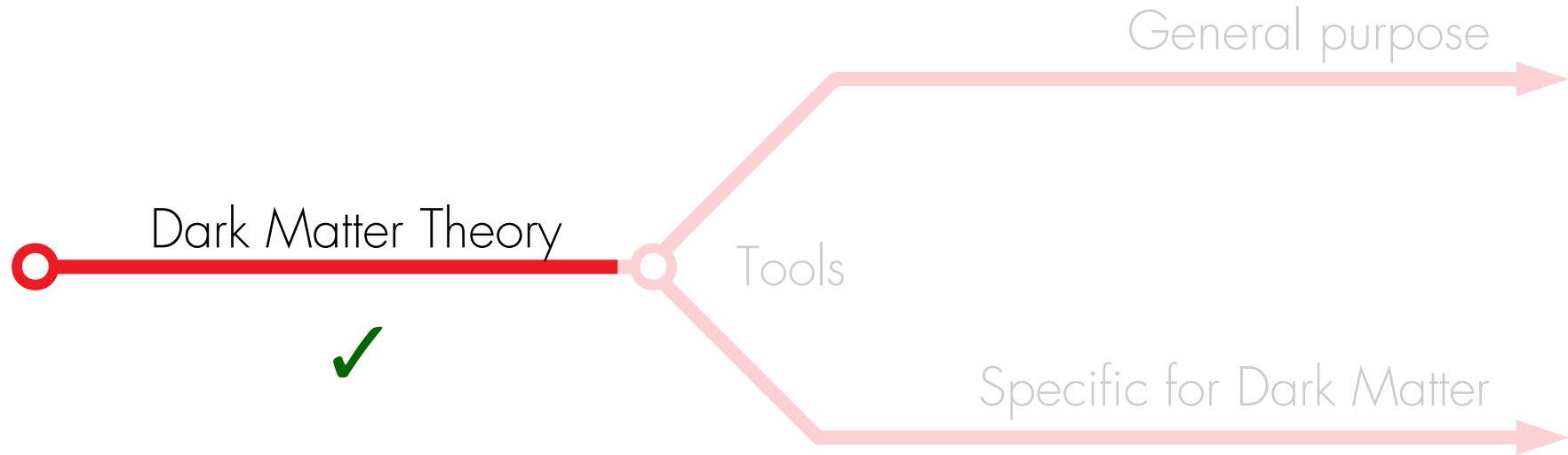
# Singlet-Triplet Scotogenic DM



# Singlet-Triplet Scotogenic DM



# Course plan



Tomorrow!  
codes!



# Thanks